

Markus Elsing

Tracking at the LHC (Part 0)

- Introduction and Outline of Lecture Series

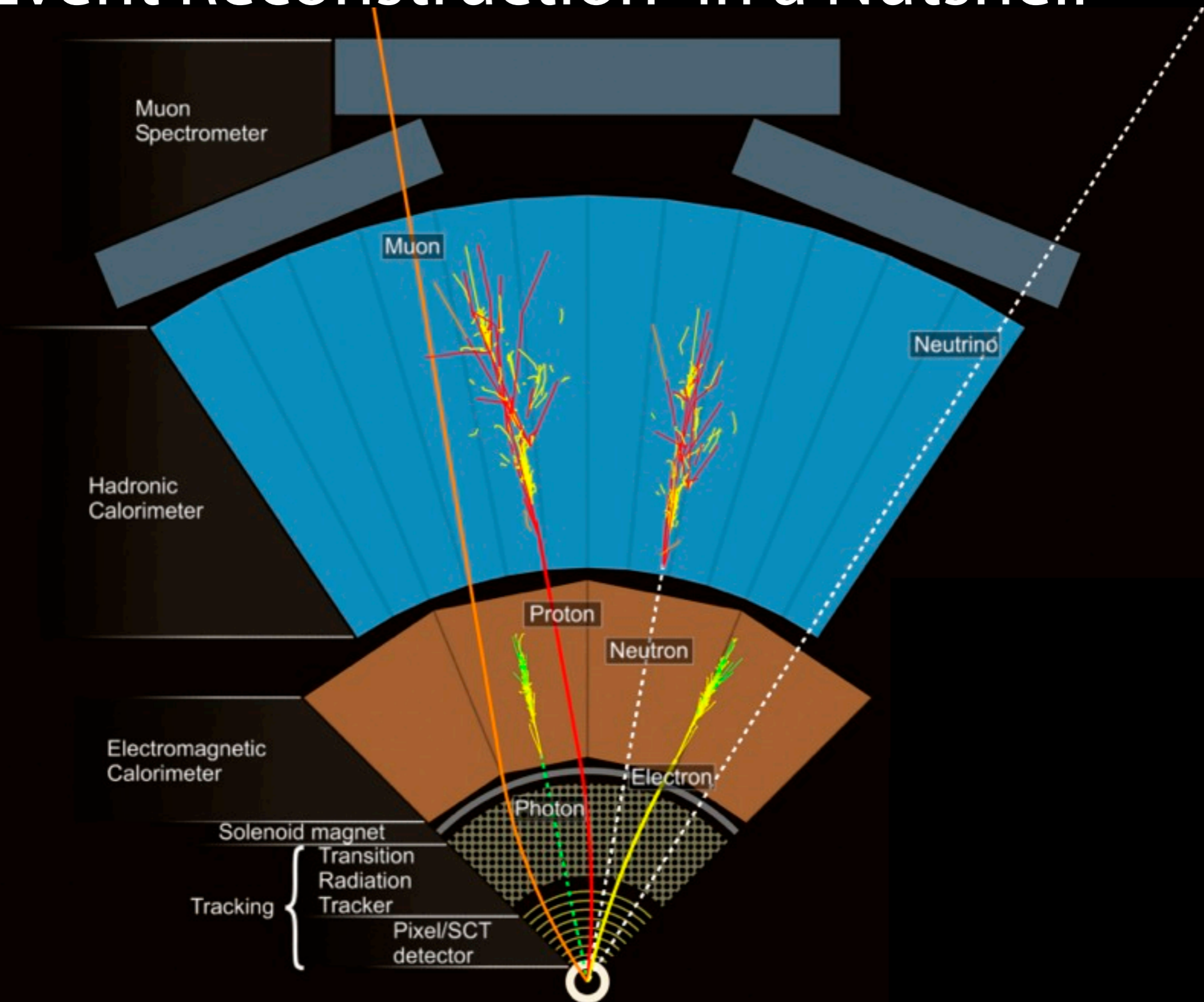


Introduction

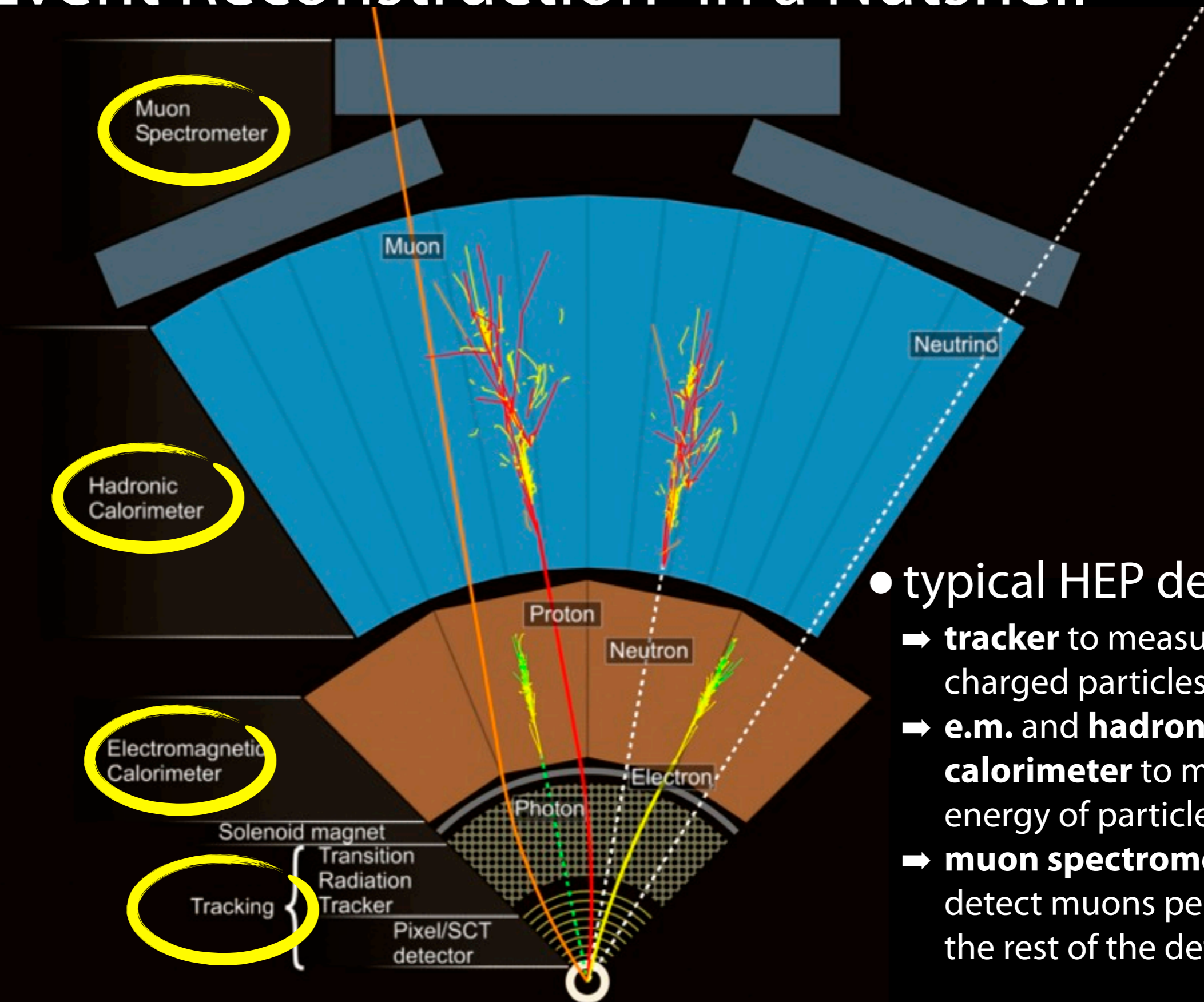
- broad **physics program** covered by **LHC** experiments
 - ➔ 2 general purpose pp experiments (ATLAS and CMS)
cover: SM QCD/W/Z/top, Higgs, SUSY, Exotics, (b-physics) ...
 - ➔ LHCb as dedicated b-physics experiment (forward physics)
 - ➔ ALICE as a heavy ion experiment
- **detectors** designed to optimize physics performance
 - ➔ at design luminosities ($10^{34} \text{ cm}^{-2}\text{s}^{-1}$) and pileup (~ 23 min.bias events)
 - ➔ b-physics trigger (LHCb)
 - ➔ heavy ion "central" event multiplicities (ALICE)
- task of **event reconstruction** is to identify objects
 - ➔ e/ μ / τ leptons, photons, (b) jets, missing E_T , exclusive hadronic states...
 - ➔ input to physics analysis of complete event signature



Event Reconstruction “in a Nutshell”



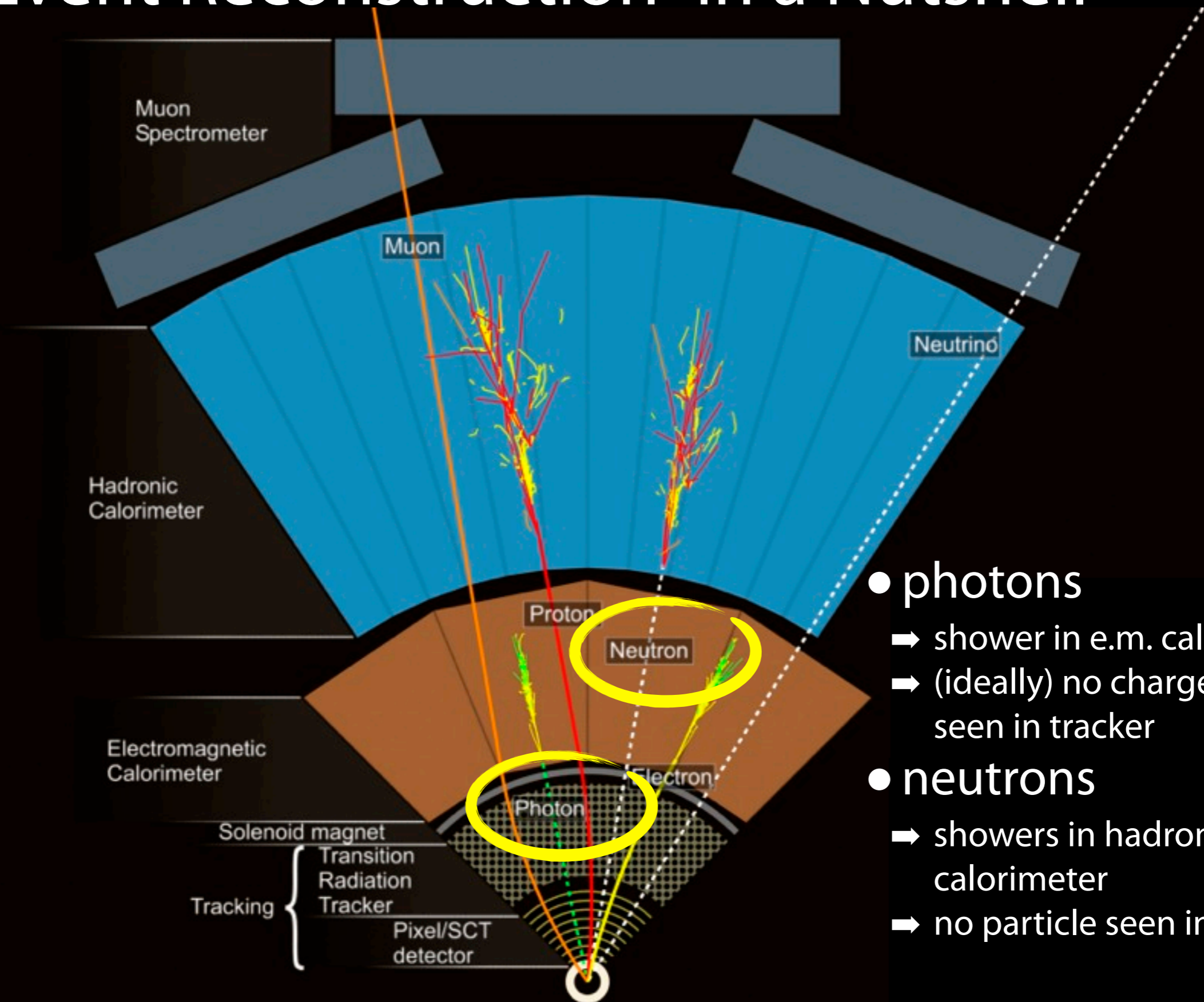
Event Reconstruction "in a Nutshell"



- typical HEP detector
 - ➔ **tracker** to measure charged particles
 - ➔ **e.m. and hadronic calorimeter** to measure energy of particles (jets)
 - ➔ **muon spectrometer** to detect muons penetrating the rest of the detector

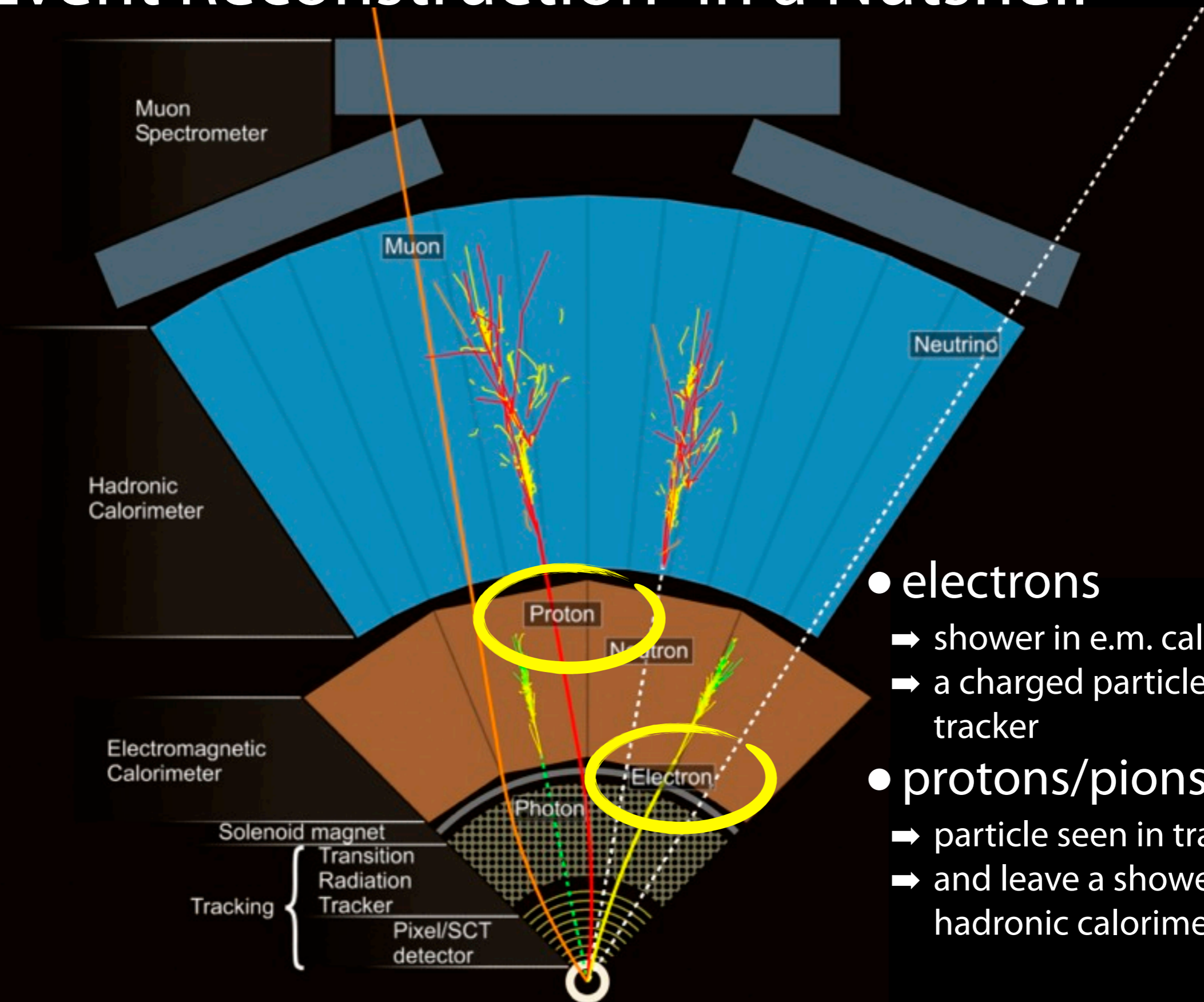


Event Reconstruction "in a Nutshell"



- photons
 - ➔ shower in e.m. calorimeter
 - ➔ (ideally) no charged particle seen in tracker
- neutrons
 - ➔ showers in hadronic calorimeter
 - ➔ no particle seen in tracker

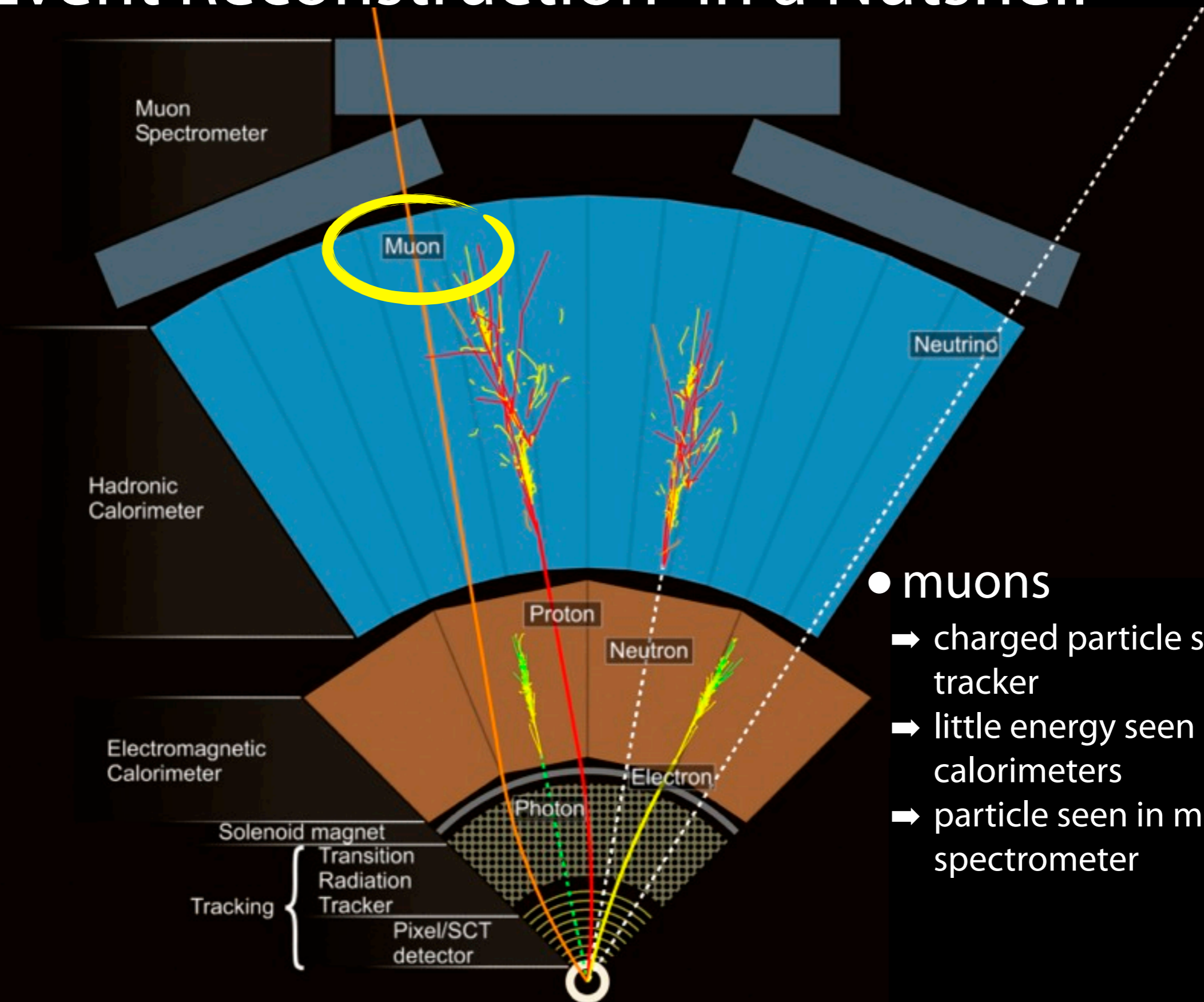
Event Reconstruction “in a Nutshell”



- electrons
 - ➔ shower in e.m. calorimeter
 - ➔ a charged particle seen in tracker
- protons/pions
 - ➔ particle seen in tracker
 - ➔ and leave a showers in hadronic calorimeter



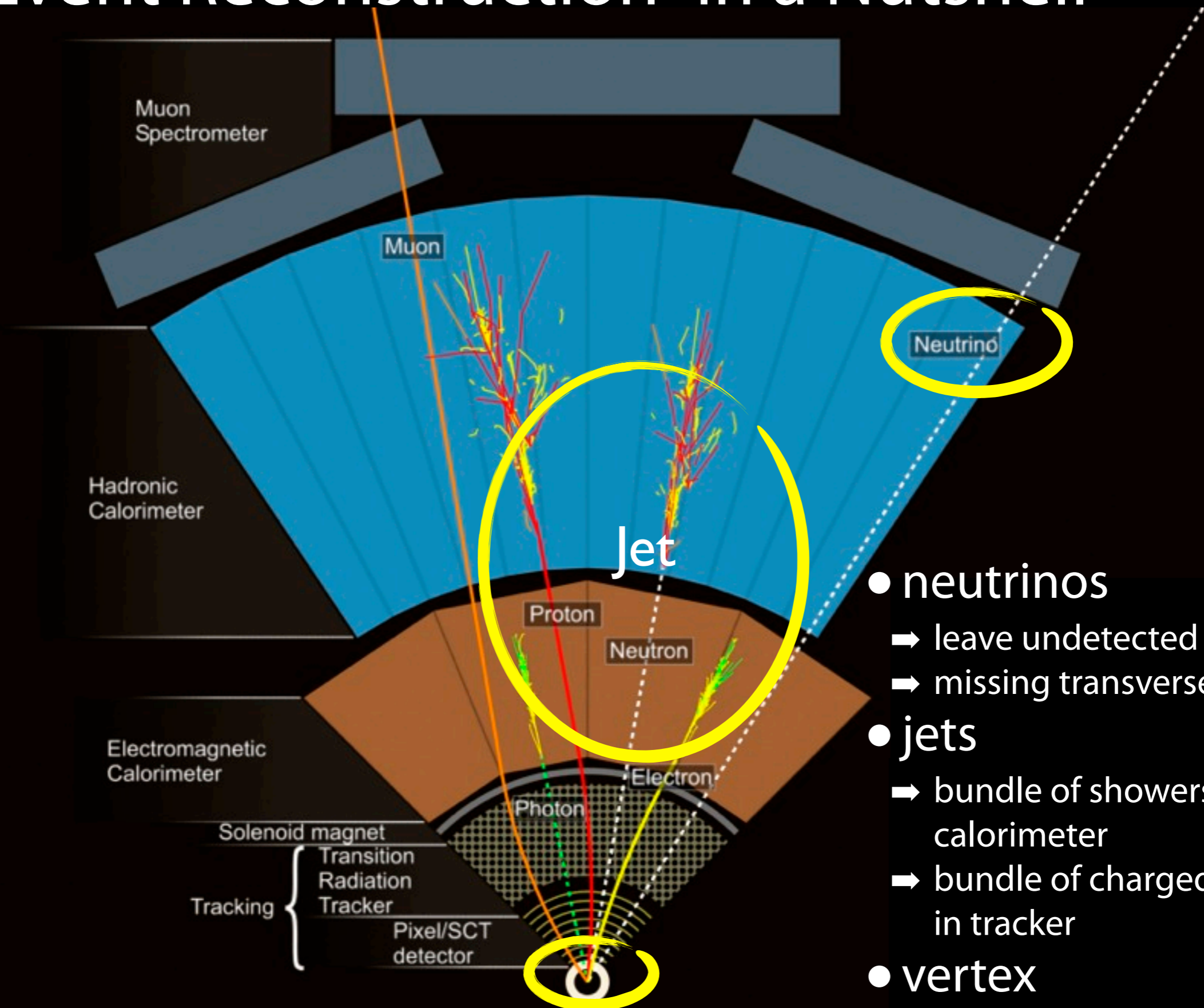
Event Reconstruction "in a Nutshell"



- muons
 - ➔ charged particle seen in tracker
 - ➔ little energy seen in calorimeters
 - ➔ particle seen in muon spectrometer



Event Reconstruction "in a Nutshell"

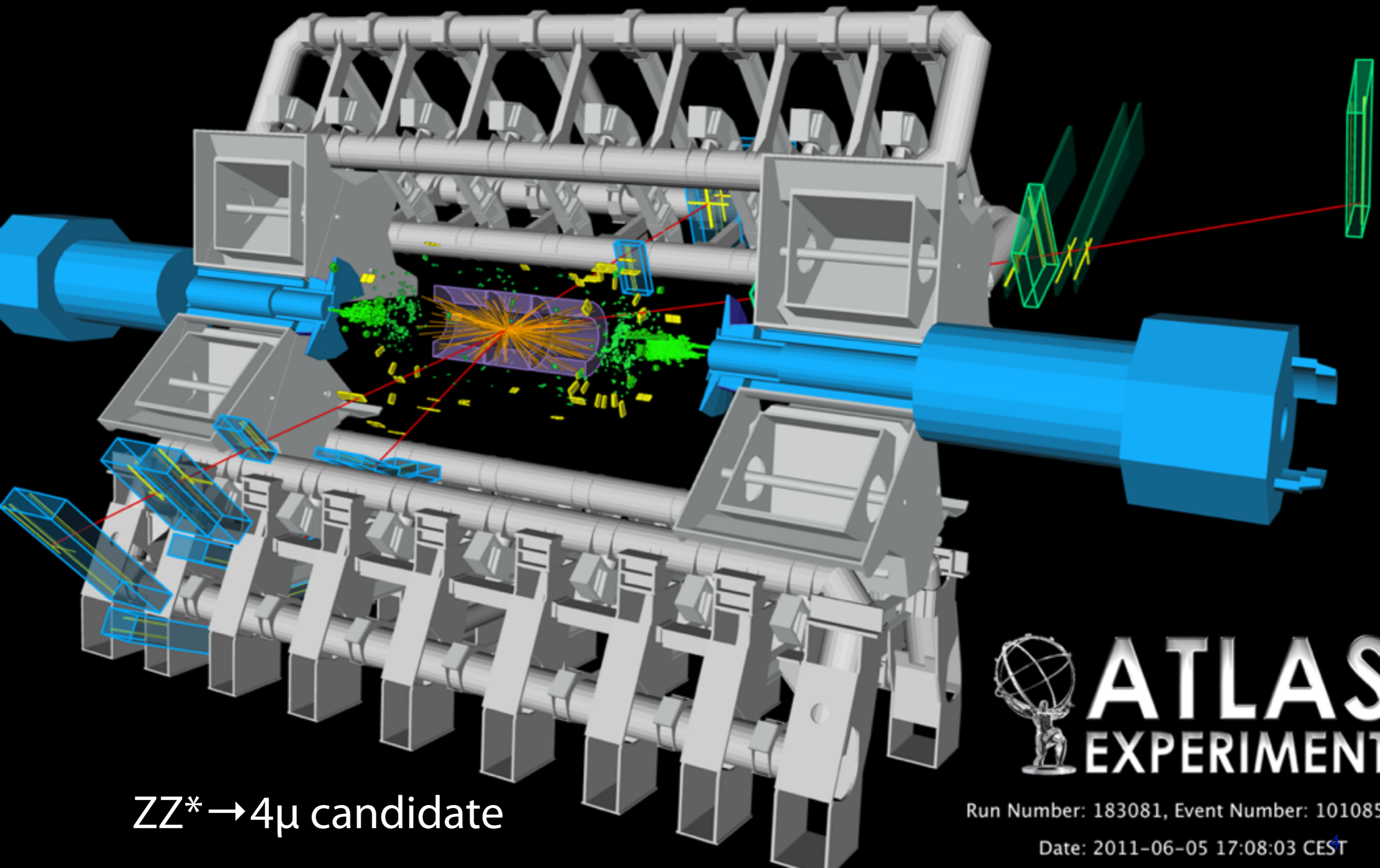


- neutrinos
 - ➔ leave undetected
 - ➔ missing transverse energy
- jets
 - ➔ bundle of showers in calorimeter
 - ➔ bundle of charged particles in tracker
- vertex



In Reality ?

... a bit more complicated



$ZZ^* \rightarrow 4\mu$ candidate



ATLAS
EXPERIMENT

Run Number: 183081, Event Number: 10108572

Date: 2011-06-05 17:08:03 CEST

Tracking at the LHC

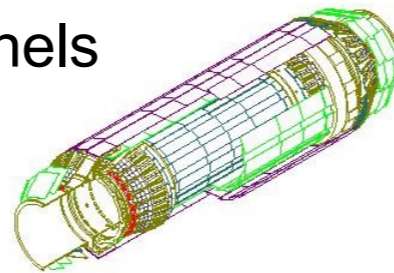
- object reconstruction to cover LHC physics program
 - ➔ often requires **combining information** from tracking detector with calorimetric and muon spectrometer measurements
 - ➔ **TRACKING** is a central aspect of the event reconstruction and analysis
- requirements on tracking detectors
 - ➔ **precision tracking** at LHC luminosities (central heavy ion event multiplicities) with a hermitic detector
 - ➔ usually Pixel/Strip Detector for precise **primary/secondary vertex** reconstruction and to provide excellent **b-tagging in jets**
 - ➔ reconstruction of **electrons** (and converted photons)
 - ➔ tracking of **muons** combined with muon spectrometer, good resolution over the full accessible momentum range
 - ➔ enable (hadronic) **tau**, exclusive **b-** and **c-hadron** reconstruction
 - ➔ provide **particle identification**, e.g.:
 - transition radiation in ATLAS TRT/ALICE TRD for electron identification
 - dE/dx in Pixels/Silicon or ALICE TPC, Cherenkov detectors (LHCb)
 - ➔ not to forget: enable fast tracking for **(high level) trigger**



Evolution of (Silicon) Detectors

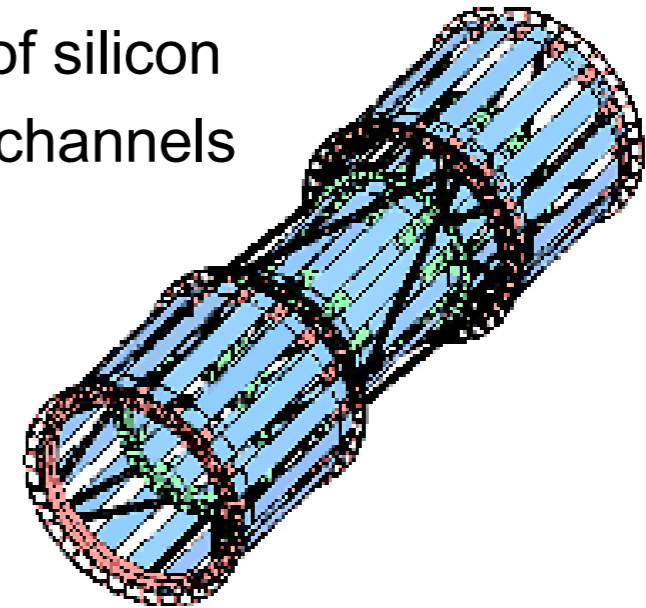
- LEP eg. DELPHI (1996)

- 1.8 m² of silicon
- 175k readout channels



- CDF SVX IIa (2001)

- 6 m² of silicon
- 175k channels



- CMS tracker

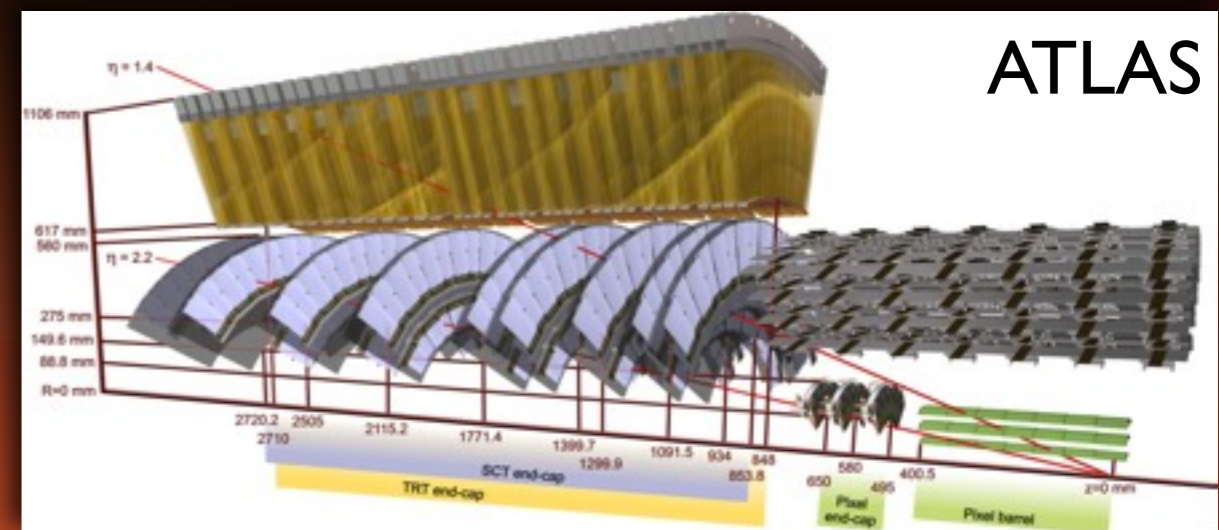
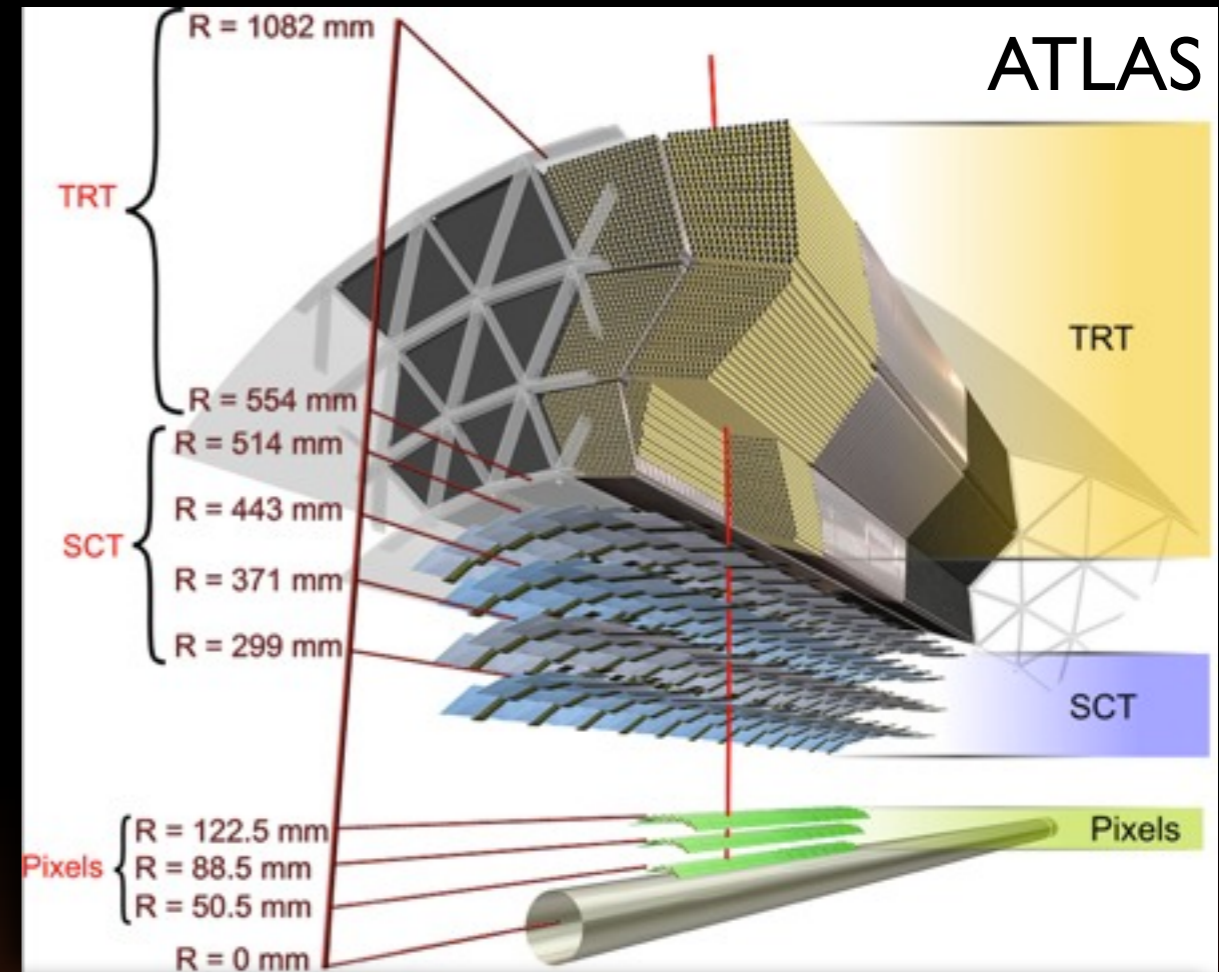
- full silicon tracker
- 210 m² of silicon
- 10.7 M channels

P.Wells

➔ results from huge technology advancements to match requirements of every generation of experiments

Example for an LHC Tracking Detector

- answer of the experiments to match physics requirements
- ATLAS:
 - ➔ 3 layer **Pixel** system, 3 endcap disks
 - 1744 Pixel modules
 - 80.4 million channels
 - pitch $50 \mu\text{m} \times 400 \mu\text{m}$
 - total of 1.8 m^2
 - ➔ 4 layers of small angle stereo strips, 9 endcap disks each side (**SCT**)
 - 4088 double sided modules
 - 6.3 million channels
 - pitch $80 \mu\text{m}$, 40 mrad stereo angle
 - total of 60 m^2
 - ➔ Transition Radiation Tracker (**TRT**)
 - typically 36 hits per track
 - transition radiation to identify electrons
 - total of 370K drift tubes



Outline of Lectures on next 3 Days

- part 1 ~ Passage of Particles through Matter
- part 2 ~ LHC Tracking Detectors
- part 3 ~ Concepts for Track Reconstruction
- part 4 ~ Vertex Reconstruction and its Applications
- part 5 ~ Commissioning, Alignment and Performance
- part 6 ~ High Luminosity and Upgrade



Feedback Welcome !

- first time I give this lecture series
 - ➔ after years in this field I may take things for granted which in reality are technicalities that need to be explained
- will try to give a balanced overview on tracking and vertexing relevant for all LHC experiments
- material presented is probably biased towards ATLAS
 - ➔ easier for me to find the relevant plots, etc.



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CREDITS: tanks for help and material from...

A.Salzburger, G.Herten, D.Froidevaux, M.Hauschild, P.Wells, W.Riegler, R.Mankel, T.Cornelissen, A.Poppleton, A.Strandli, R.Frühwirth, G.Piacquadio, A.Morley and several others I should mention here



Markus Elsing

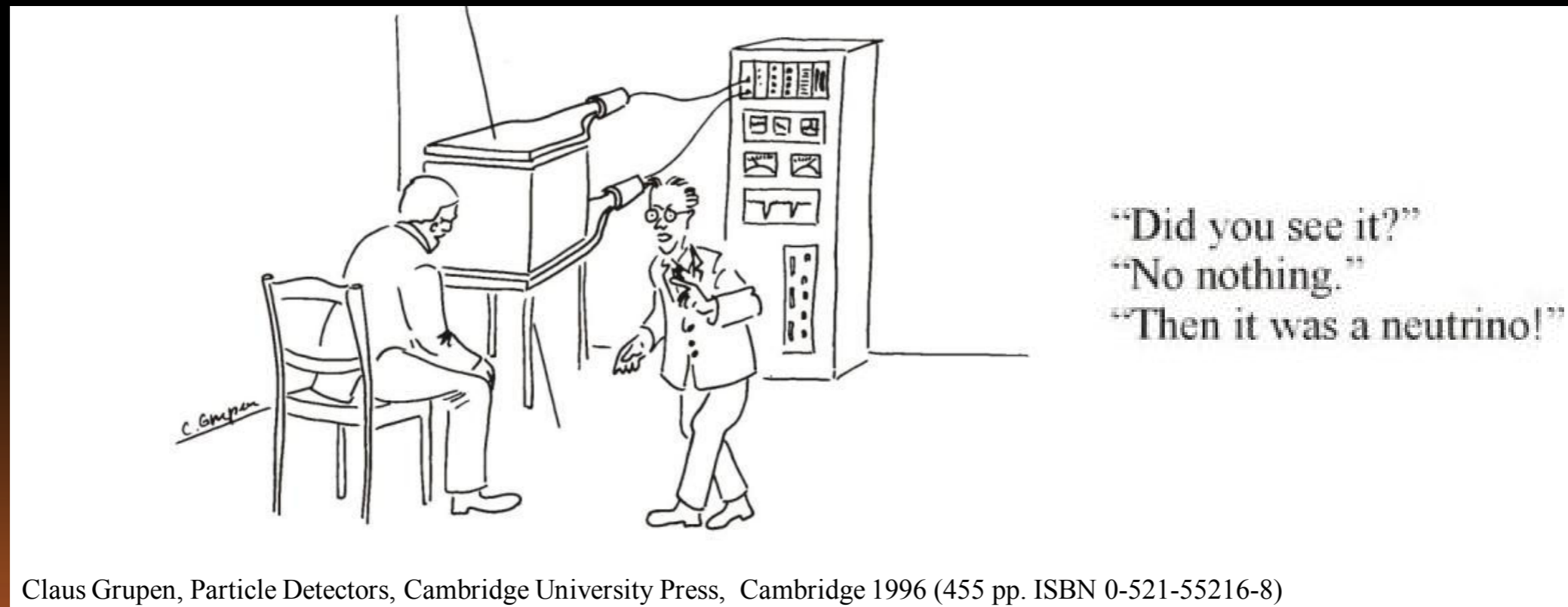
Tracking at the LHC (Part 1)

- Passage of Particles through Matter



Passage of Particles through Matter

- any device that is to detect a particle must interact with it in some way
 - ➔ well, almost...
 - ➔ in many experiments neutrinos are measured by missing transverse momentum



Outline of Part 1

- overview of charged particle interactions with matter
 - ➔ provide not only the means to detect charged particles
- important as well to understand they affect the tracking performance of
 - ➔ energy loss
 - ➔ multiple scattering
 - ➔ Bremsstrahlung
 - ➔ hadronic interactions



Charged Particle Interactions with Matter

- particles are detected through their interaction with the active detector materials

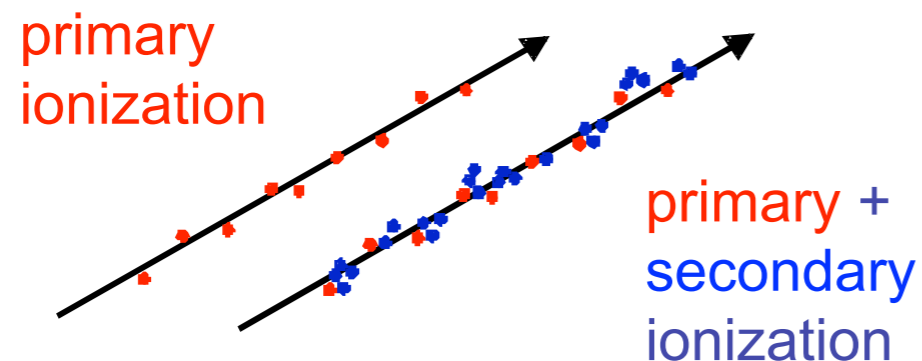


Charged Particle Interactions with Matter

■ particles are detected through their interaction with the active detector materials

■ **energy loss by ionization**

primary ionisation can generate secondary ionisation



typically:

total ionization $\approx 3 \times$ primary ionization

➡ ~ 90 electrons/cm in gas at 1 bar

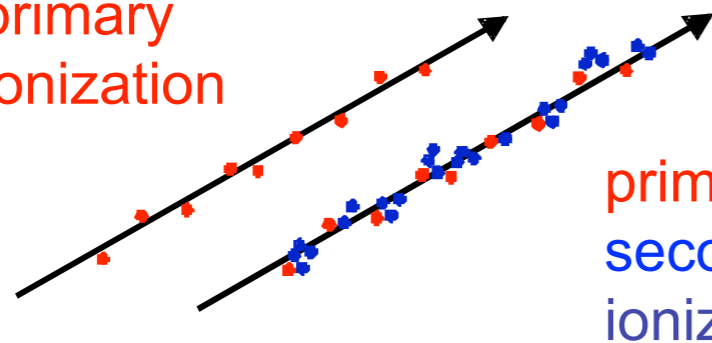
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primary ionization

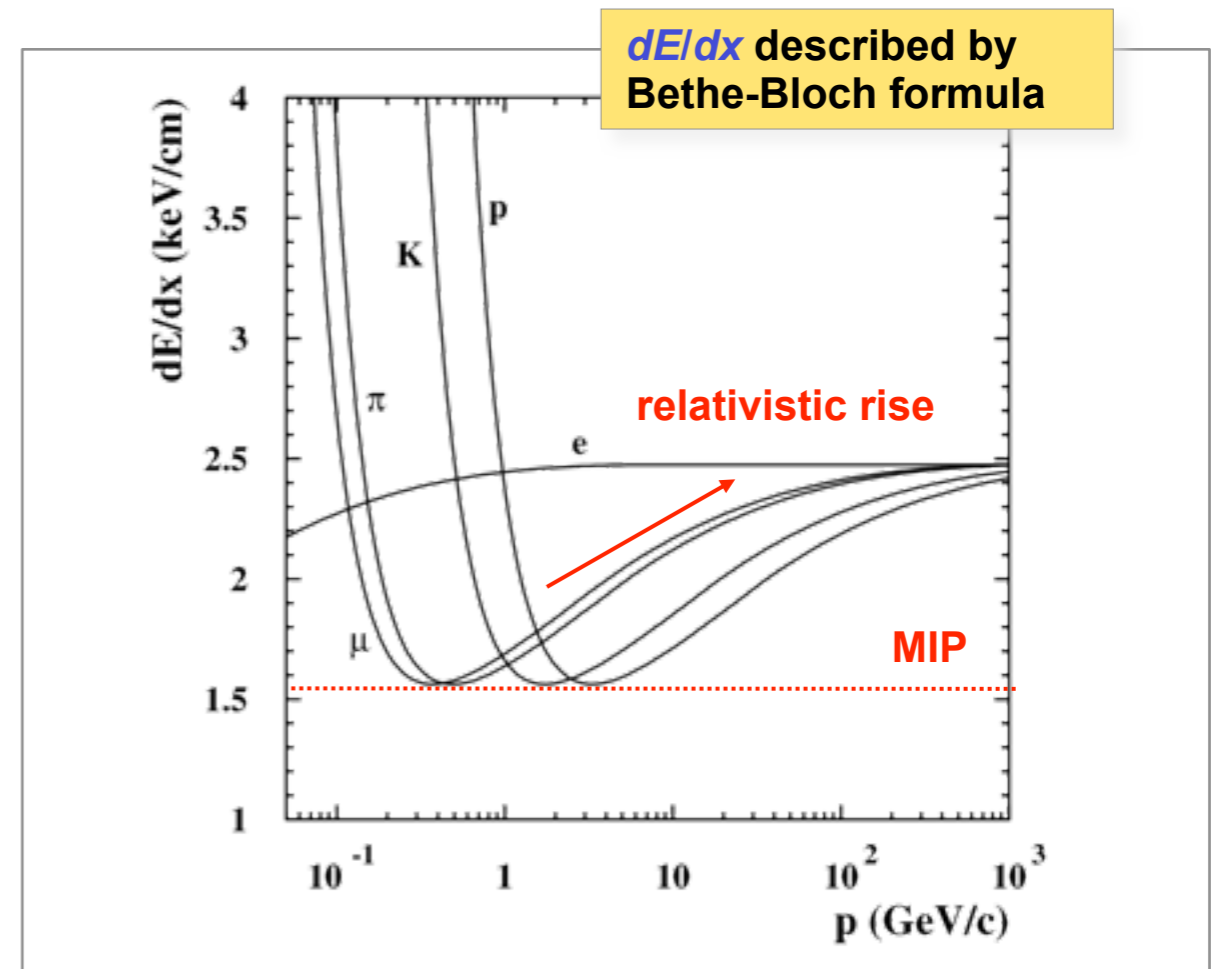


primary + secondary ionization

typically:

total ionization $\approx 3 \times$ primary ionization

➡ ~ 90 electrons/cm in gas at 1 bar



➡ not directly used for particle identification by ATLAS/CMS

Charged Particle Interactions with Matter

- particles are detected through their interaction with the active detector materials
 - energy loss by ionisation



Charged Particle Interactions with Matter

- particles are detected through their interaction with the active detector materials
 - energy loss by ionisation
 - **Bremsstrahlung**

due to interaction with Coulomb field of nucleus

dominant energy loss mechanism for electrons down to low momenta (~ 20 MeV)

initiates EM cascades (showers)

Charged Particle Interactions with Matter

- particles are detected through their interaction with the active detector materials
 - Energy loss by ionization
 - Bremsstrahlung



Charged Particle Interactions with Matter

- particles are detected through their interaction with the active detector materials
 - Energy loss by ionization
 - Bremsstrahlung
 - **multiple scattering**

charged particles traversing a medium are deflected by many successive small-angle scatters

angular distribution ~ Gaussian

$$\sigma_{MS} \sim 1/p * (x/X_0)^{1/2}$$

but also large angles from Rutherford scattering $\sim \sin^{-4}(\theta/2)$

➔ complicates track fitting, limits momentum measurement

Charged Particle Interactions with Matter

- particles are detected through their interaction with the active detector materials
 - energy loss by ionization
 - Bremsstrahlung
 - multiple scattering



Charged Particle Interactions with Matter

■ particles are detected through their interaction with the active detector materials

- energy loss by ionization
- Bremsstrahlung
- multiple scattering
- **radiation length**

material thickness in detector is measured in terms of dominant energy loss reactions at high energies:

- Bremsstrahlung for electrons
- pair production for photons

definition:

X_0 = length over which an electron loses all but $1/e$ of its energy by bremsstrahlung

= $7/9$ of mean free path length of photon before pair production

describe material thickness in units of X_0



Charged Particle Interactions with Matter

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describe material thickness in units of X_0

material	X_0 [cm]
Be	35.3
Carbon-fibre	~ 25
Si	9.4
Fe	1.8
PbWO ₄	0.9
Pb	0.6

↑
ATLAS LAr
absorber

↑
CMS ECAL
crystals



Charged Particle Interactions with Matter

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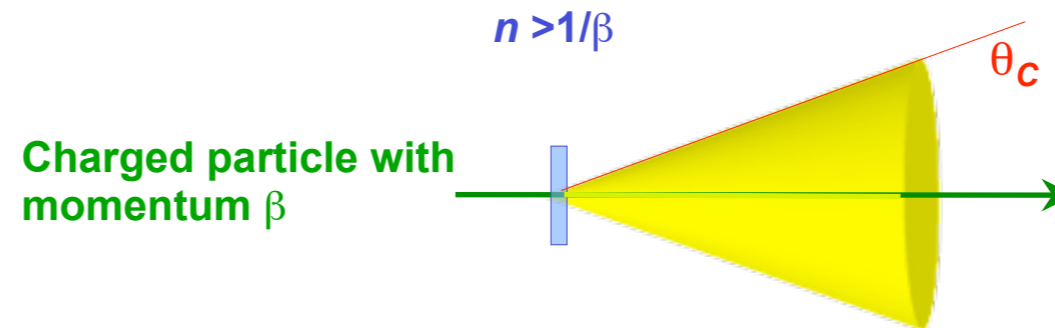


Charged Particle Interactions with Matter

■ particles are detected through their interaction with the active detector materials

- energy loss by ionisation
- Bremsstrahlung
- multiple scattering
- radiation length
- **Cherenkov radiation**

a relativistic charge particle traversing a dielectric medium with refraction index $n > 1/\beta$ emits Cherenkov radiation in cone with angle θ_C around track: $\cos\theta_C = (n\beta)^{-1}$



light cone emission when passing thin medium

detector types RICH (LHCb), DIRC, Aerogel counters (not employed by ATLAS/CMS))

Charged Particle Interactions with Matter

■ particles are detected through their interaction with the active detector materials

■ energy loss by ionization

■ Bremsstrahlung

■ multiple scattering

■ radiation length

■ Cherenkov radiation

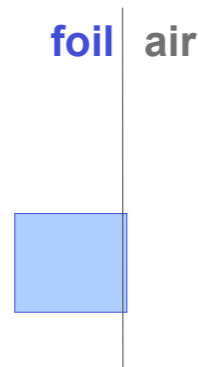


Charged Particle Interactions with Matter

■ particles are detected through their interaction with the active detector materials

- energy loss by ionization
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- radiation length
- Cherenkov radiation
- **transition radiation**

photon radiation when charged ultra-relativistic particles traverse the boundary of two different dielectric media (foil & air)

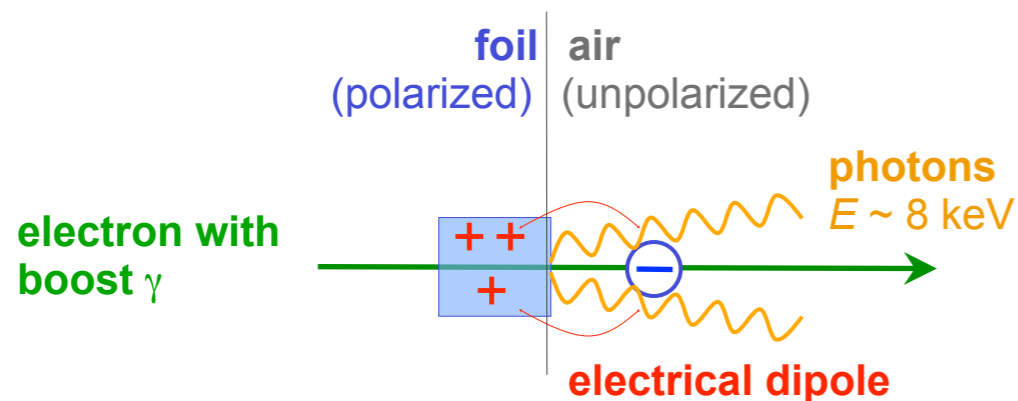


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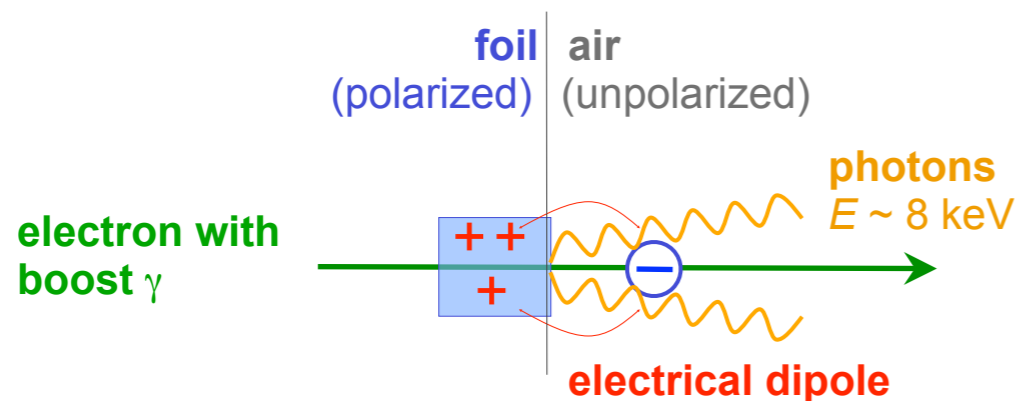
➔ significant radiation for $\gamma > 1000$
and > 100 boundaries

Charged Particle Interactions with Matter

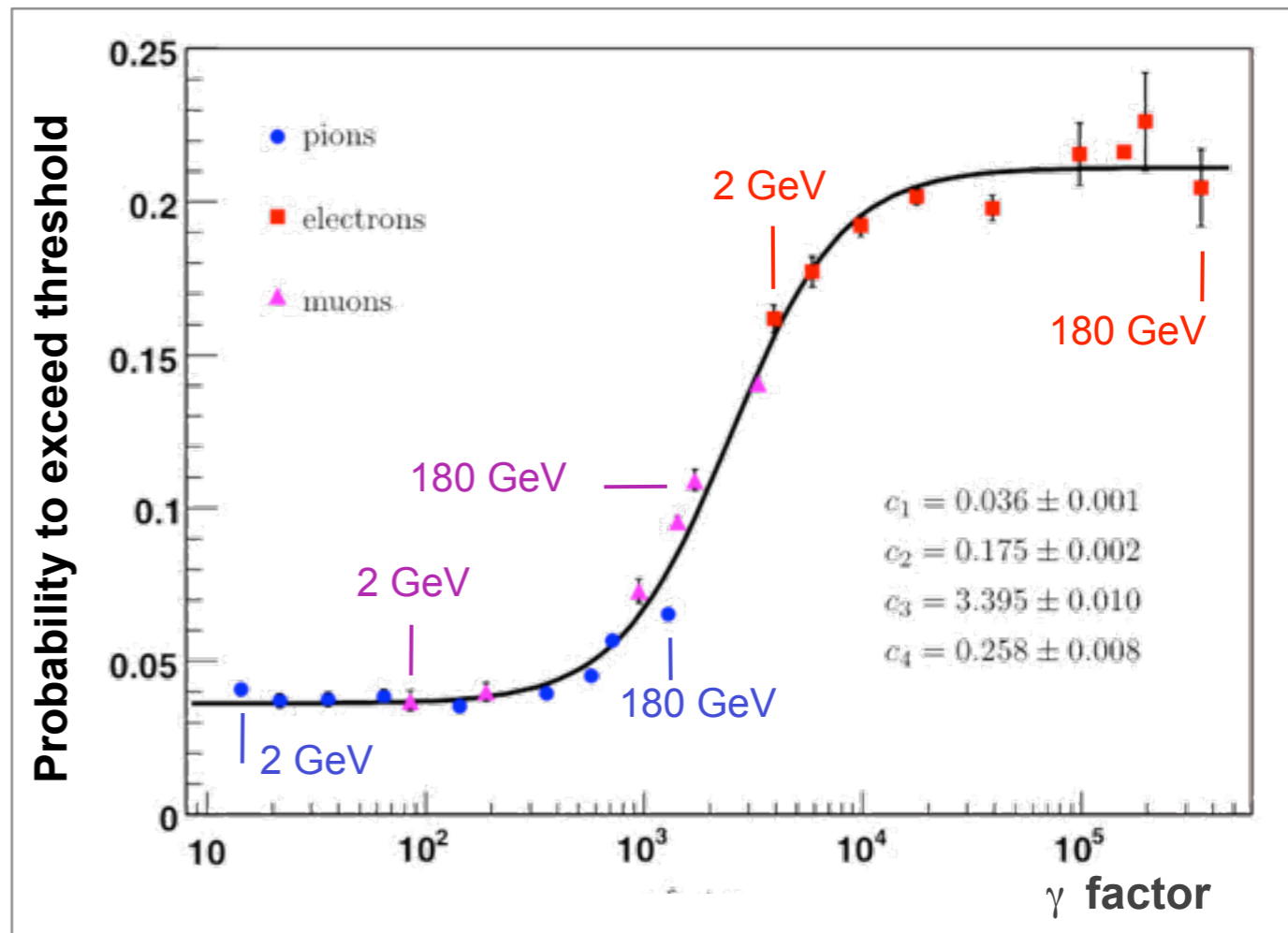
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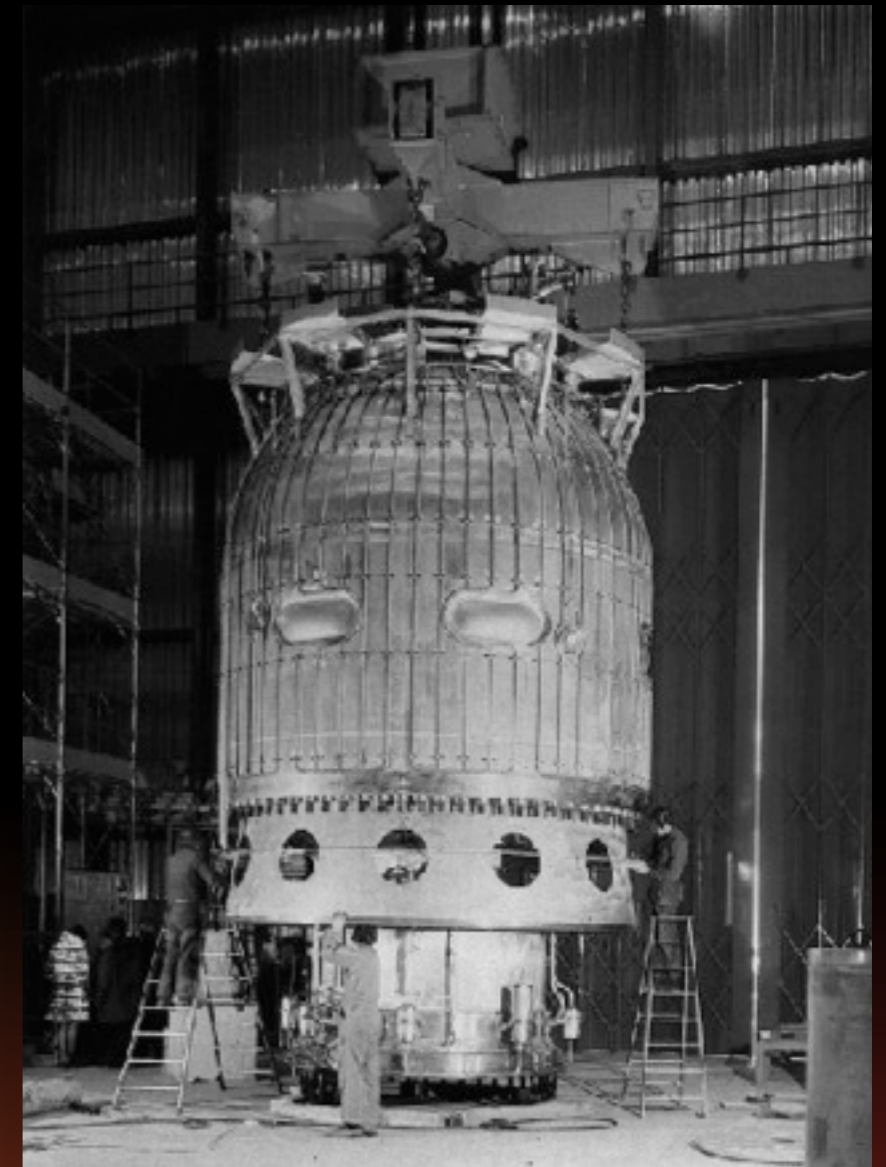
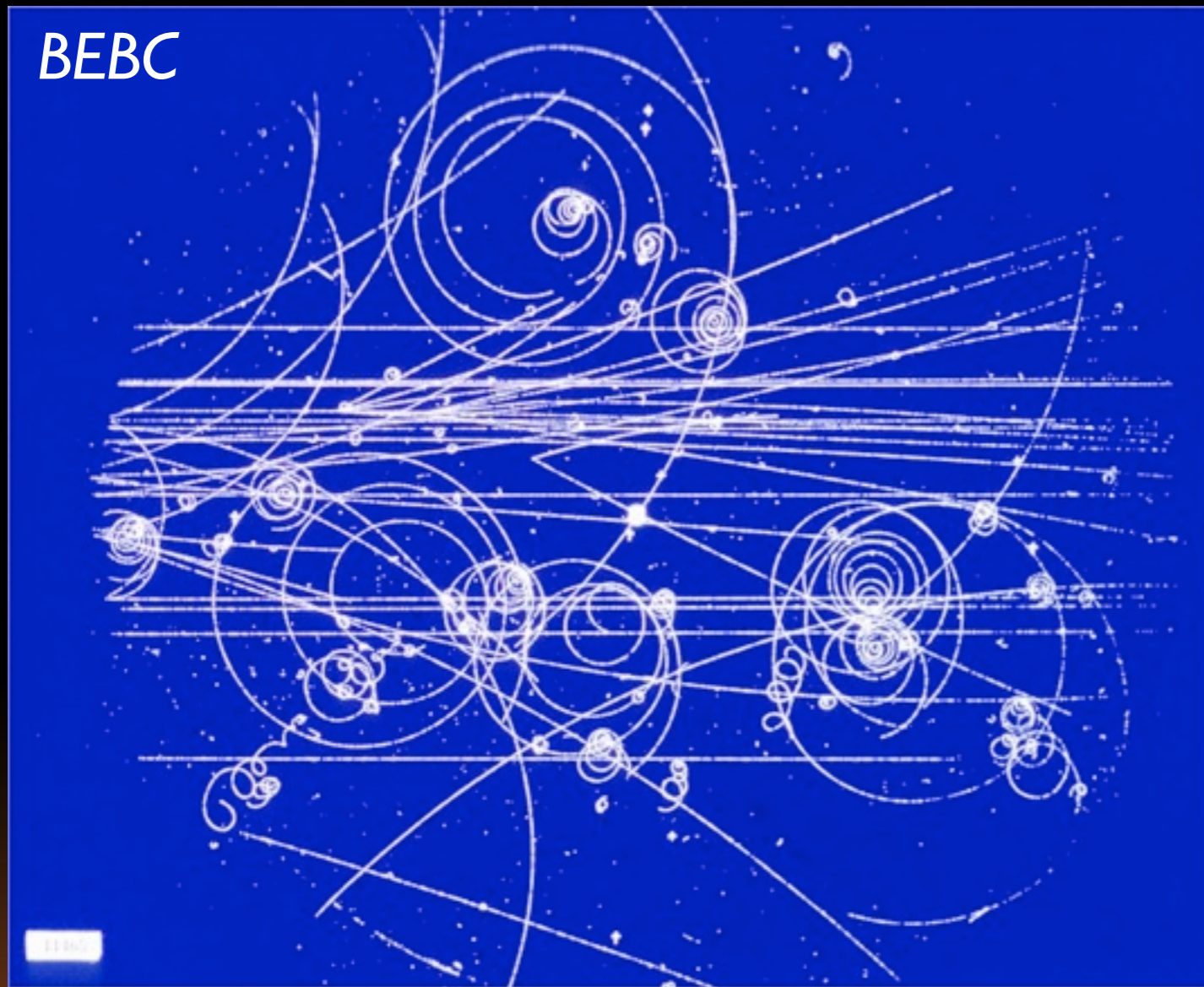
photon radiation when charged ultra-relativistic particles traverse the boundary of two different dielectric media (foil & air)



➔ significant radiation for $\gamma > 1000$ and > 100 boundaries



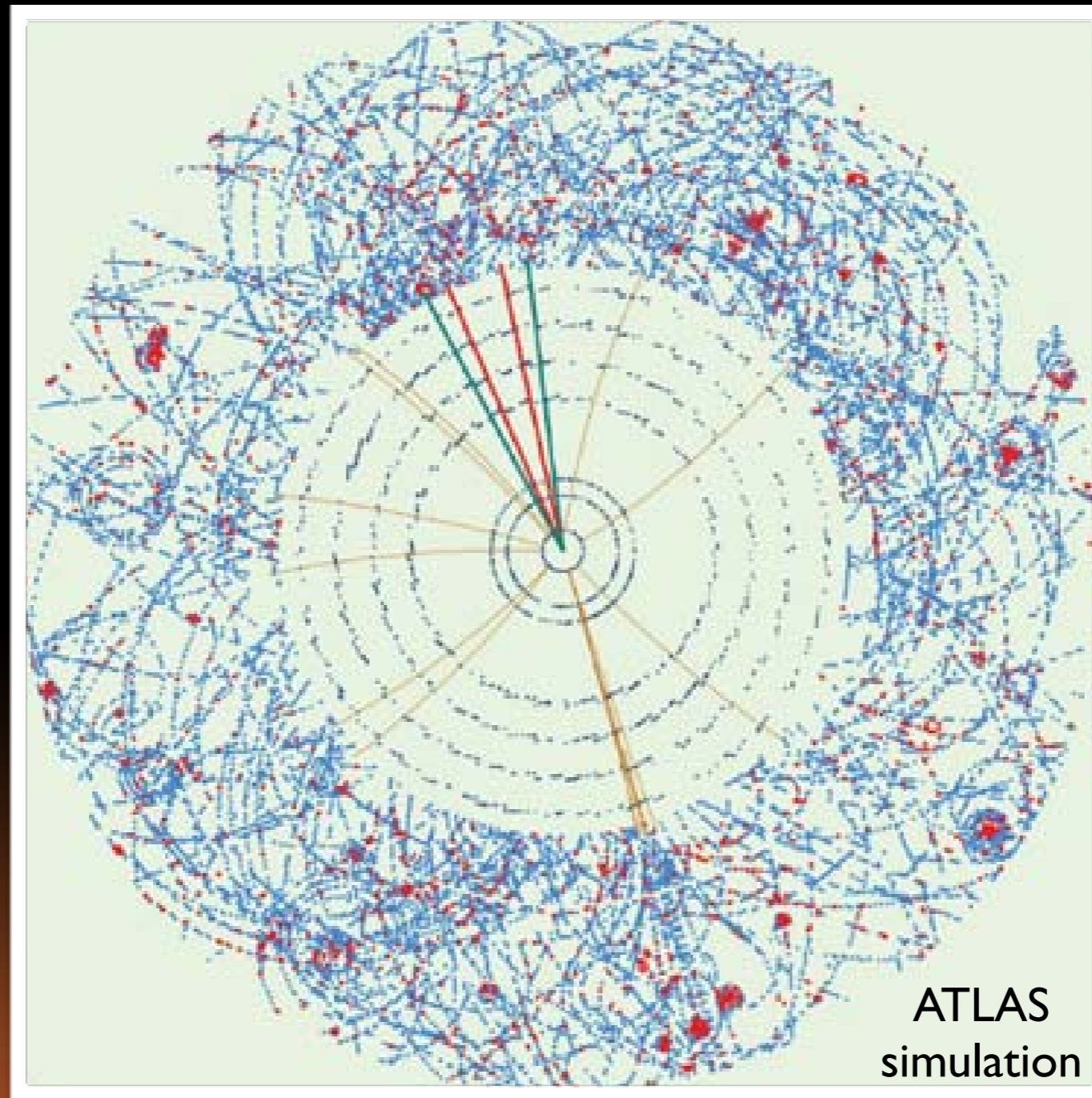
Effects are visible by Eye...



BEBC can be seen outside the Microcosm Exhibition

- give rise to beautiful old bubble-chamber photos
 - ➔ energy loss by ionization, δ -electrons, pair production, ...

... as well in modern Detectors



History of Energy Loss Calculations: dE/dx

1915: **Niels Bohr**, classical formula, Nobel prize 1922.

1930: non-relativistic formula found by **Hans Bethe**

1932: relativistic formula by **Hans Bethe**

Bethe's calculation is leading order in perturbation theory, thus only z^2 terms are included.

additional corrections:

- z^3 corrections calculated by **Barkas+Andersen**
- correction calculated by **Felix Bloch** (Nobel prize 1952, for nuclear magnetic resonance). Although the formula is called Bethe-Bloch formula the z^4 term is usually not included.
- shell corrections: atomic electrons are not stationary
- density corrections: by **Enrico Fermi** (Nobel prize 1938, for discovery of nuclear reaction induced by slow neutrons)



Hans Bethe
1906-2005

Born in Strasbourg, emigrated to US in 1933. Professor at Cornell U. Nobel prize 1967 for theory of nuclear processes in stars.



The Bethe-Bloch Formula

$$-\left\langle \frac{dE}{dx} \right\rangle = K z^2 \frac{Z}{A} \frac{1}{\beta^2} \left[\frac{1}{2} \ln \frac{2m_e c^2 \beta^2 \gamma^2 T_{\max}}{I^2} - \beta^2 - \frac{\delta(\beta\gamma)}{2} \right]$$

→ characteristics of the energy loss as a function of the particle velocity ($\beta\gamma$)

→ with

- z ~ charge of incident particle
- Z ~ atomic number of absorber
- A ~ atomic mass of absorber

$$\frac{K}{A} = 4\pi N_A r_e^2 m_e c^2 / A = 0.307075 \text{ MeV g}^{-1} \text{cm}^2, \text{ for } A = 1 \text{g mol}^{-1}$$

- I ~ mean excitation energy of absorber
- T_{\max} ~ maximum energy transfer in a single collision

$$T_{\max} = \frac{2m_e c^2 \beta^2 \gamma^2}{1 + 2\gamma m_e / M + (m_e / M)^2}$$

- $\delta(\beta\gamma)$ ~ density effect correction to ionization loss

→ $x = \rho s$ ~ surface density or mass thickness, with unit g/cm^2 , s is the length
(dE/dx has the units $\text{MeV cm}^2/\text{g}$)



The Bethe-Bloch Formula

Bethe-Bloch formula:

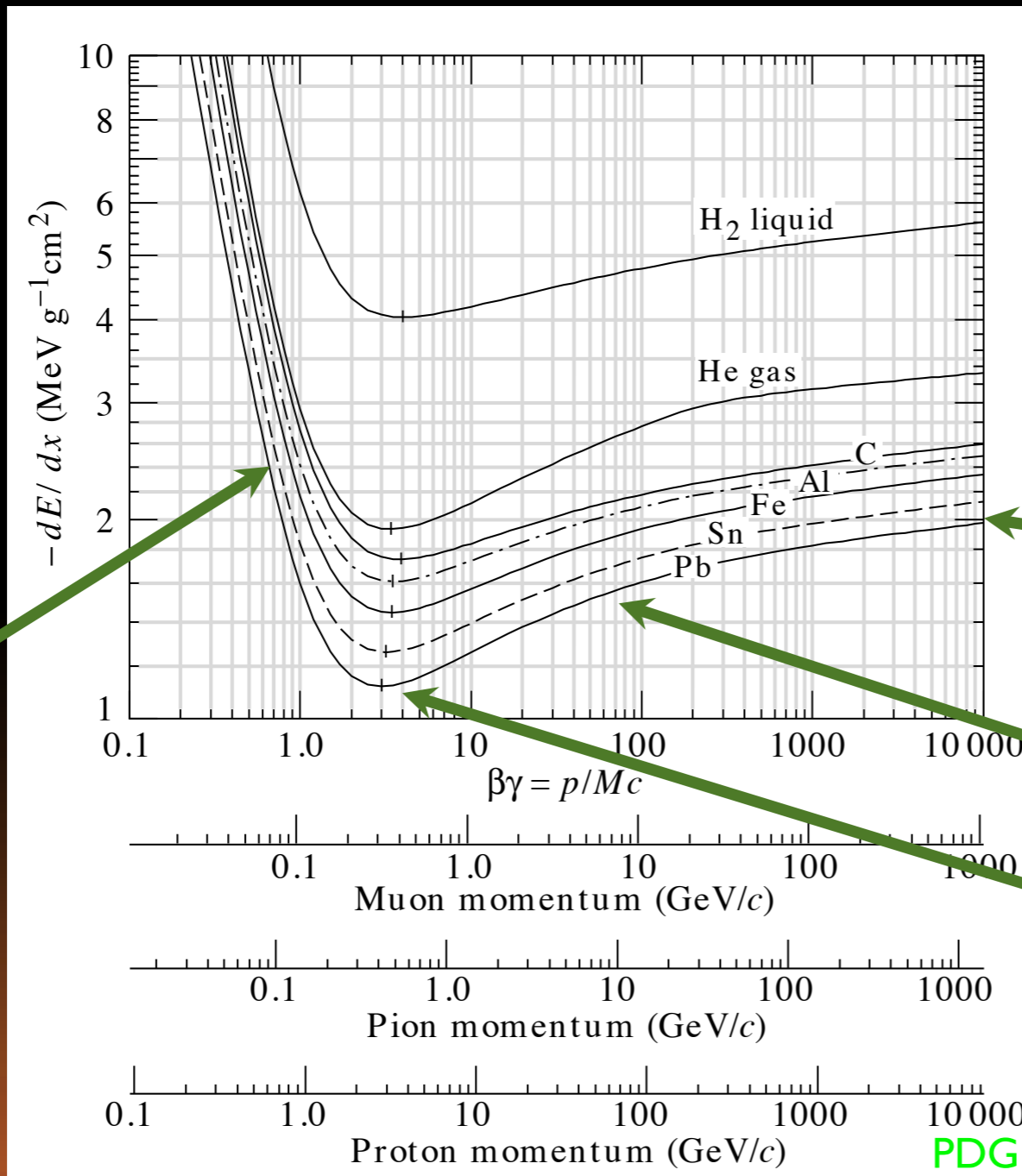
$$-\frac{dE}{dx} = K z^2 \frac{Z}{A} \frac{1}{\beta^2} \left[\frac{1}{2} \ln f(\beta) - \beta^2 - \frac{\delta(\beta\gamma)}{2} \right]$$

except in hydrogen, particles of the same velocity have similar energy loss in different materials.

Fermi plateau: density effect, polarization of medium "screens" particle charge

relativistic rise

the **minimum in ionization** occurs at $\beta\gamma = 3.0$ to 3.5 , as Z goes from 7 to 100

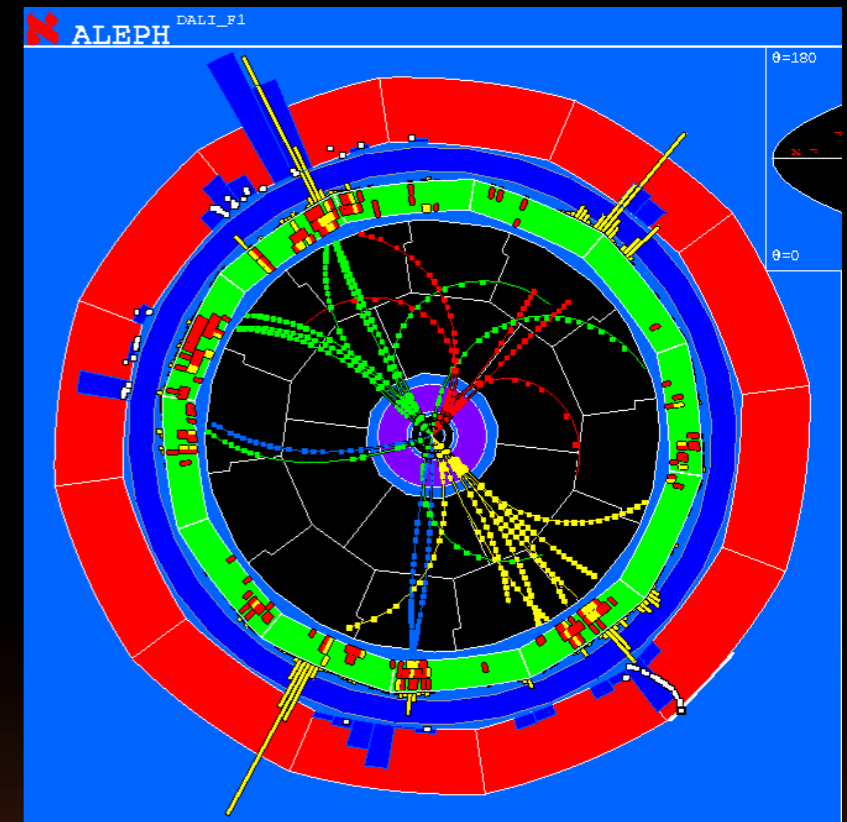
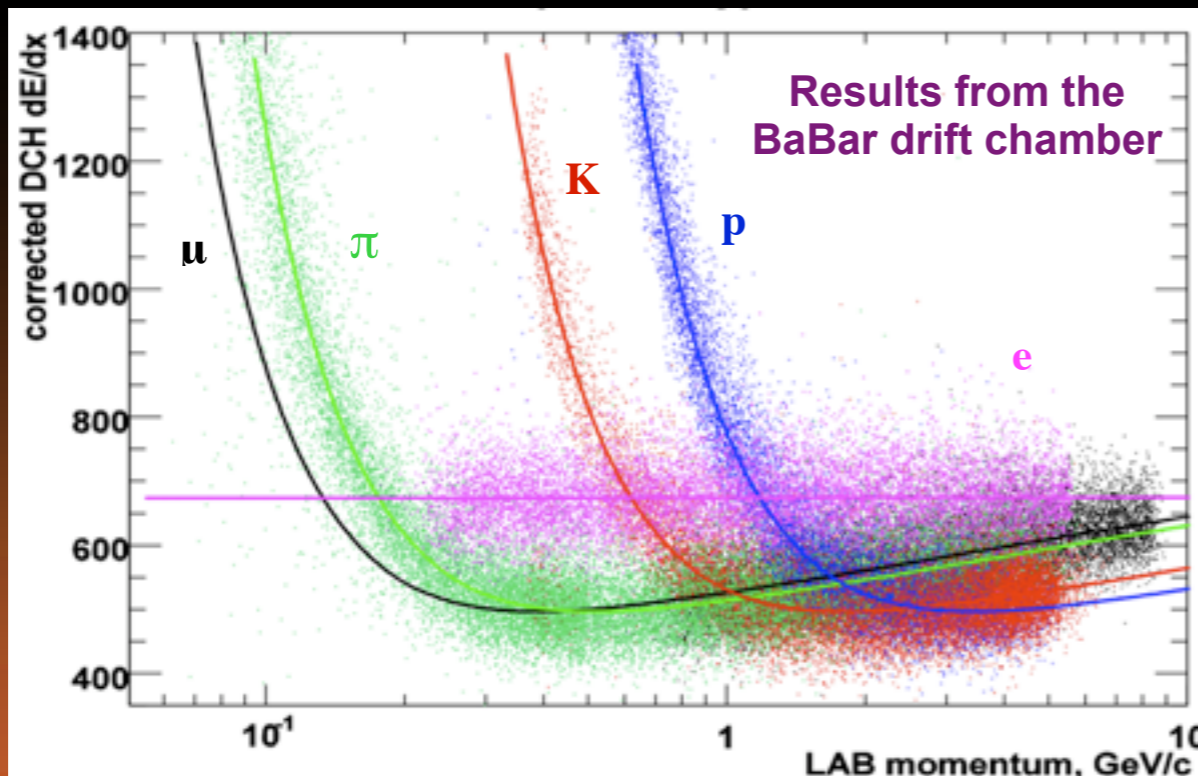


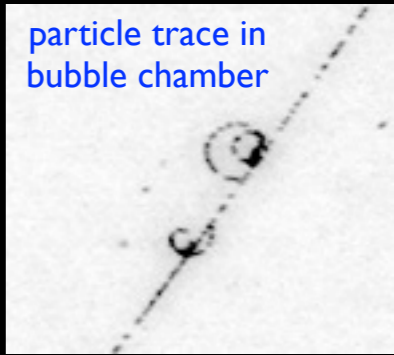
classical $1/\beta^2$ dependency (Rutherford Scattering)



Particle Identification using dE/dx

- energy loss depends on particle velocity
 - ➔ \approx independent of particle mass M
- as a function of particle momentum
 - ➔ $p = Mc\beta\gamma$ depends on particle mass !
- application in an experiment:
 - ➔ measure momentum from curvature of particle track in magnetic field
 - ➔ measure ionization along the track





particle trace in bubble chamber

Fluctuations in Energy Loss

from L. Ropelewski

Real detector (limited granularity) can not measure $\langle dE/dx \rangle$!

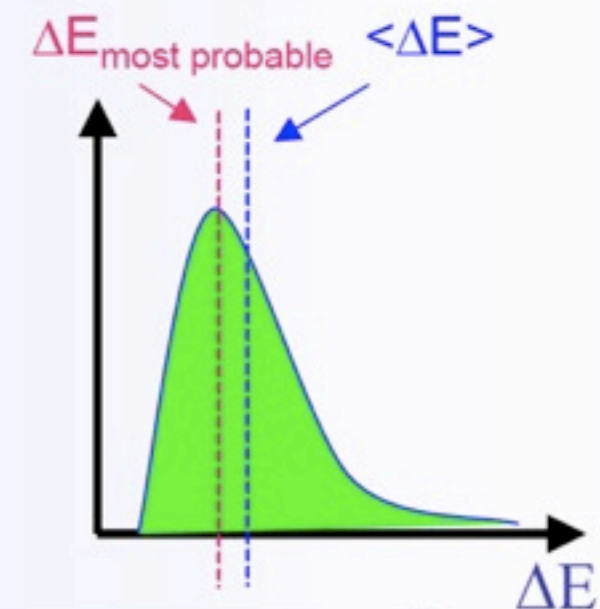
It measures the energy ΔE deposited in a layer of finite thickness δx .

For thin layers or low density materials:

→ Few collisions, some with high energy transfer.



→ Energy loss distributions show large fluctuations towards high losses: "Landau tails"

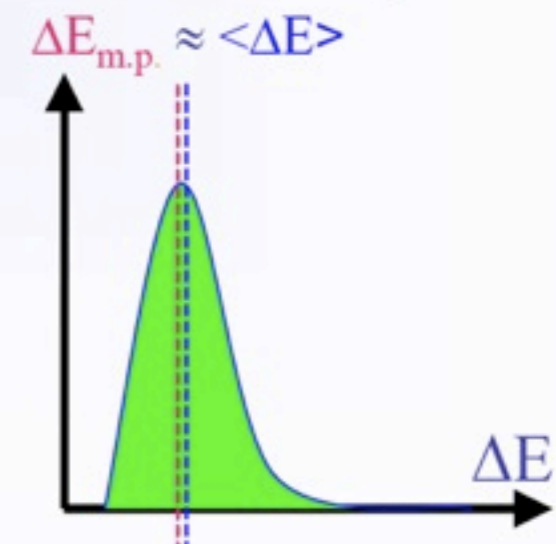
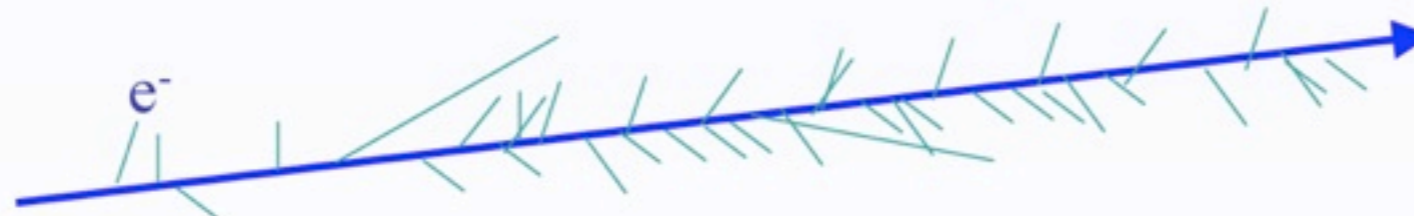


Example: Si sensor: 300 μm thick. $\Delta E_{m.p.} \sim 82 \text{ keV}$ $\langle \Delta E \rangle \sim 115 \text{ keV}$

For thick layers and high density materials:

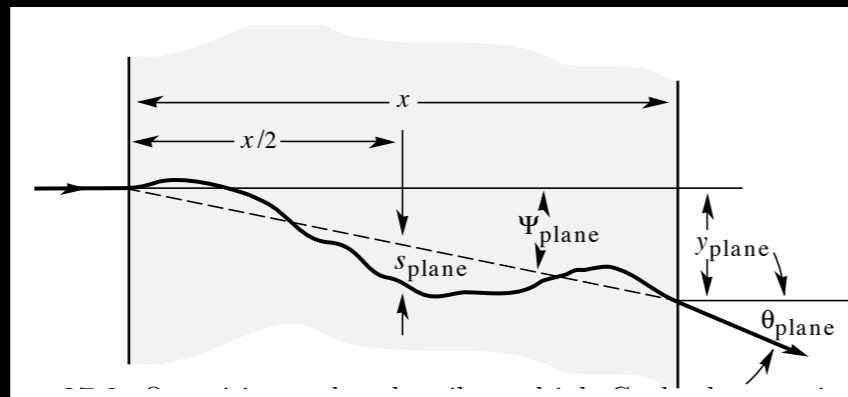
→ Many collisions.

→ Central Limit Theorem → **Gaussian shaped distributions.**



Multiple Scattering

- a particle which traverses a medium is deflected
 - ➔ by small angle **Coulomb scattering** in field of nuclei
 - ➔ for hadronic particles as well the strong interaction contributes



- **angular deflection** after traversing a distance **x**
 - ➔ described by the **Molière theory**
 - ➔ angle has roughly a Gaussian distribution, but with larger tails due to Coulomb scattering
 - ➔ Gaussian approximation

$$\Delta\Theta = \frac{13.6 \text{ MeV}}{\beta c p} z \sqrt{x/X_0} \left[1 + 0.038 \ln(x/X_0) \right]$$

- $x/X_0 \sim$ thickness of material in units of radiation length
- $z \sim$ charge of the particle

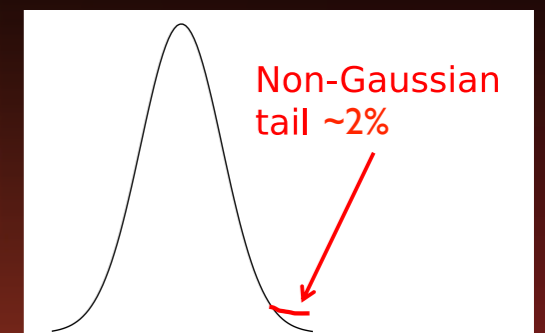


Illustration of M.S. Effect

- toy simulation
 - ➔ simulation of single particle traversing a set of individual thin material layers
 - single scattering steps accumulate

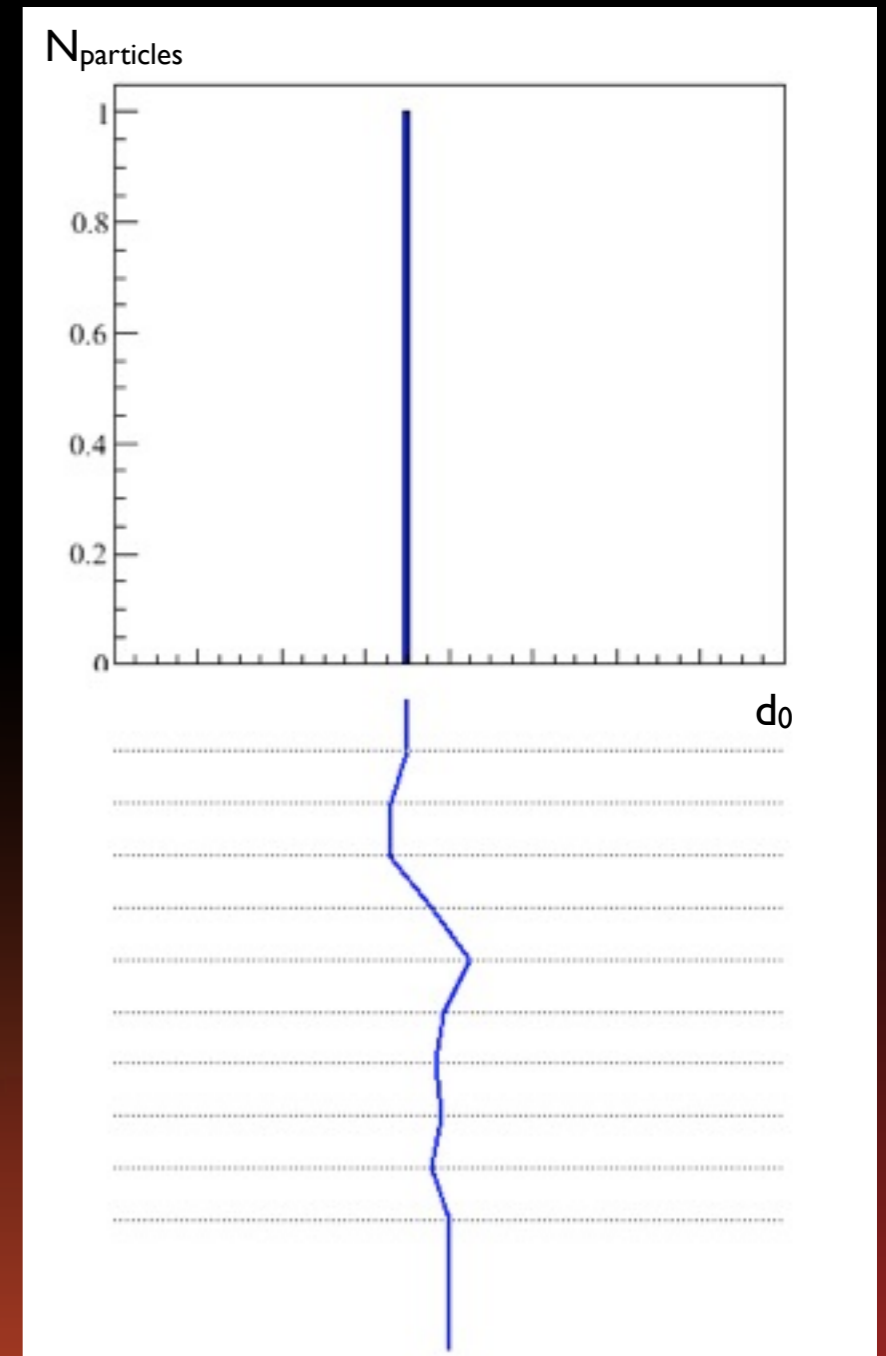
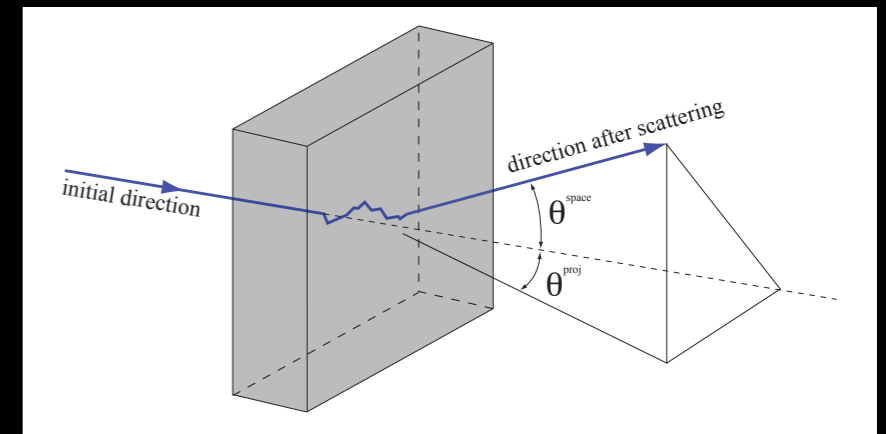


Illustration of M.S. Effect

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- ➔ simulation of single particle traversing a set of individual thin material layers
 - single scattering steps accumulate
- ➔ repeat N times:
 - central limit theorem predicts gaussian distribution

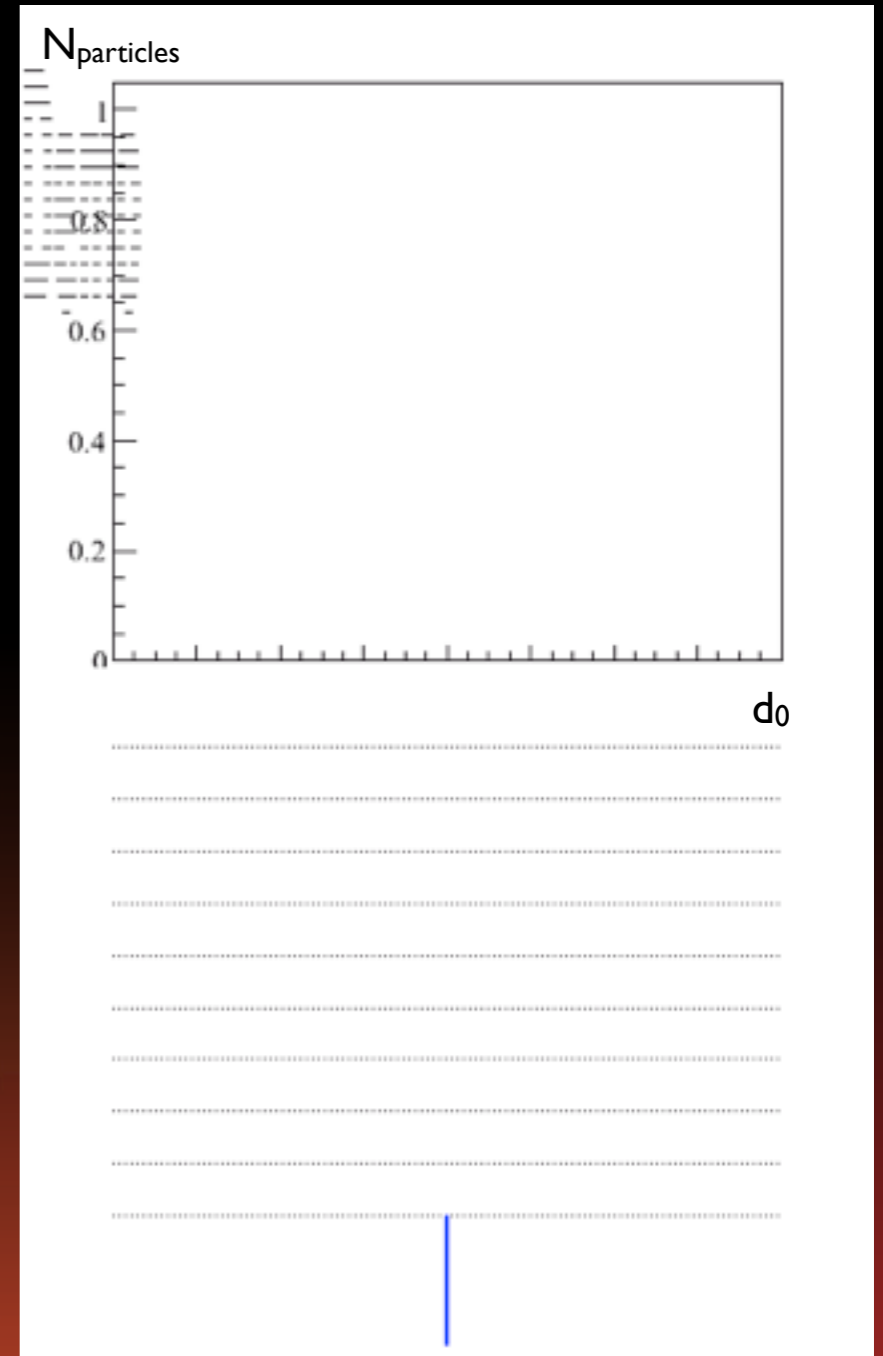
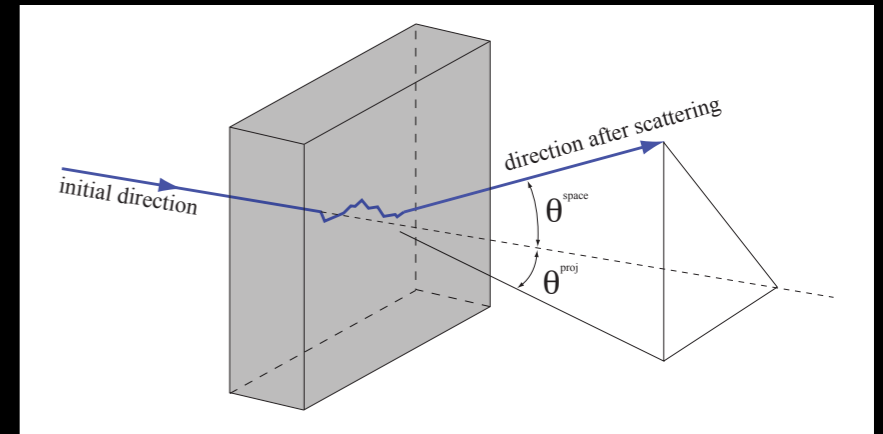
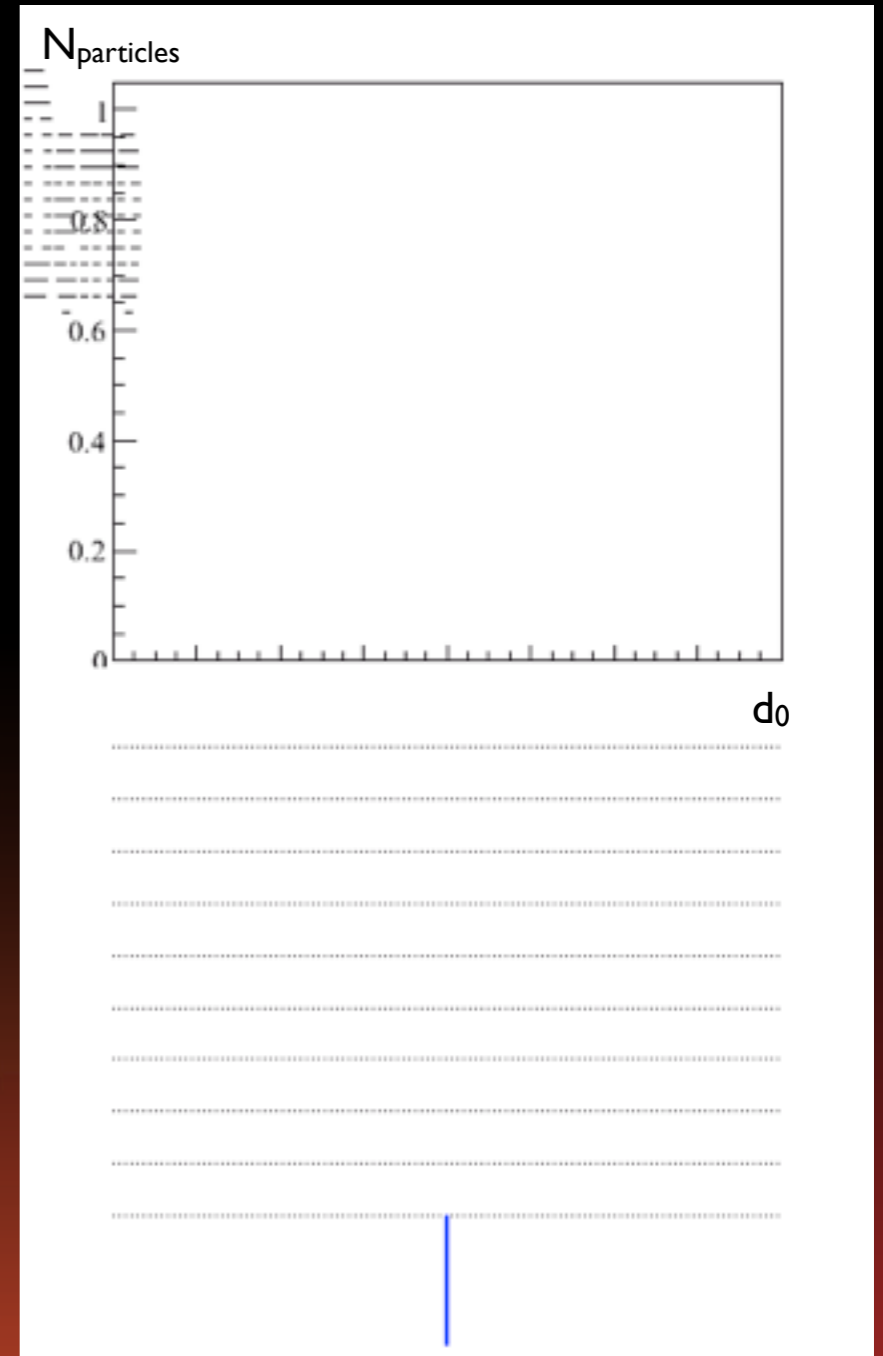
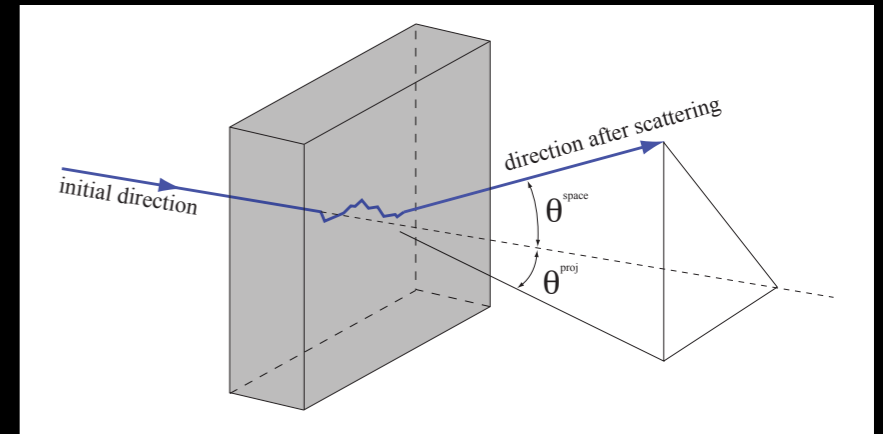


Illustration of M.S. Effect

- toy simulation
 - ➔ simulation of single particle traversing a set of individual thin material layers
 - single scattering steps accumulate
 - ➔ repeat N times:
 - central limit theorem predicts gaussian distribution
- sometimes we experience the effect



Effect on Momentum Resolution

- magnetic spectrometer

→ charged particle describes a circle in a magnetic field

$$p_T[\text{GeV}/c] = 0.3 \cdot B[\text{T}] \cdot R[\text{m}]$$

→ measure sagitta s of arc to determine curvature R

$$R = \frac{L^2}{8s} + \frac{s}{2} \approx \frac{L^2}{8s}$$

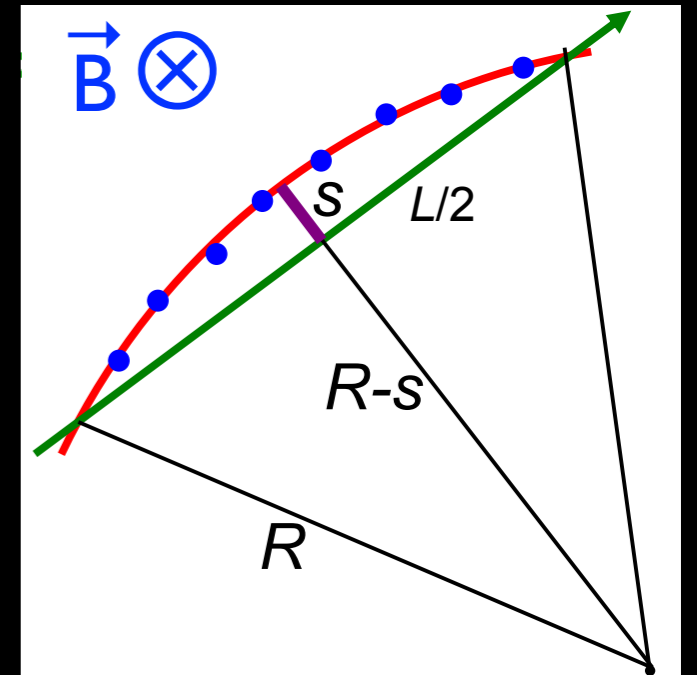
- put into upper equation results in $p_T \equiv p_T(s)$

→ relative error on momentum equals relative error on sagitta

$$\frac{\sigma_{p_T}}{p_T} = \frac{8p_T}{0.3BL^2} \sigma_s$$

→ hence relative momentum uncertainty is proportional to momentum p_T times sagitta uncertainty σ_s

→ as well, one wants large field B and long path length L



Effect on Momentum Resolution

- multiple scattering contribution to momentum uncertainty

$$\frac{\sigma_{p_T}}{p_T} = \frac{\Delta\Theta}{\Theta} \cong \frac{0.05}{BL} \sqrt{\frac{x}{X_0}}$$

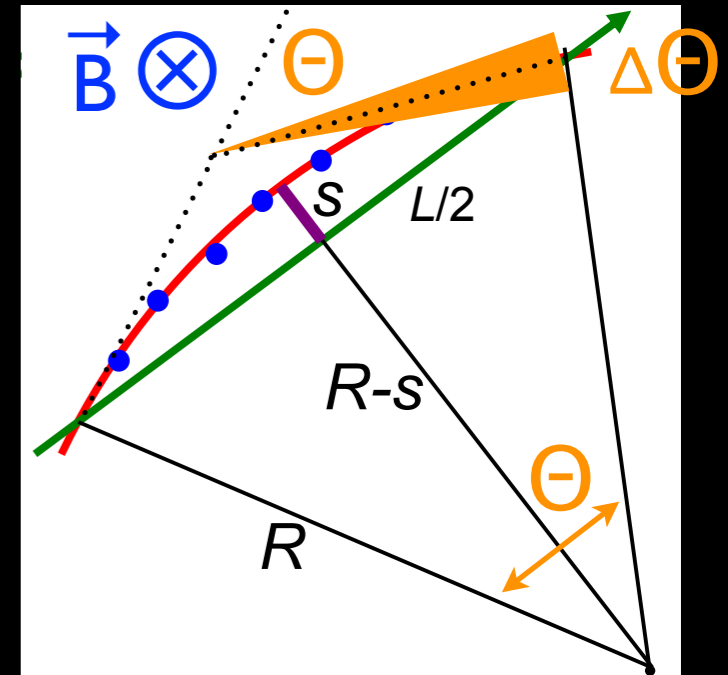
- putting things together gives

$$\frac{\sigma_{p_T}}{p_T} = \frac{8p_T\sigma_s}{0.3BL^2} \oplus \frac{0.05}{BL} \sqrt{\frac{x}{X_0}} \approx a p_T \oplus b$$

- ➔ **a** ~ resolution term dominating at high p_T
- b** ~ multiple scattering term limiting at low p_T
- ➔ sagitta uncertainly from **N** points, each with resolution $\sigma_{R\phi}$

$$\sigma_s = \sqrt{\frac{A_N}{N+4} \frac{\sigma_{R\phi}}{8}}$$

Statistical factor $A_N = 720$:
(Gluckstern)



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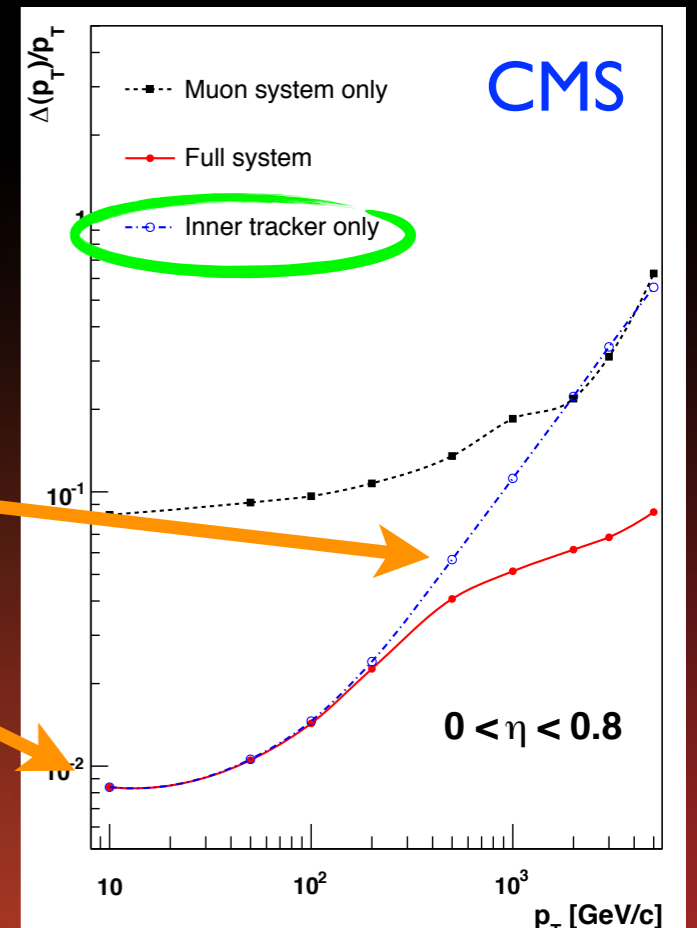
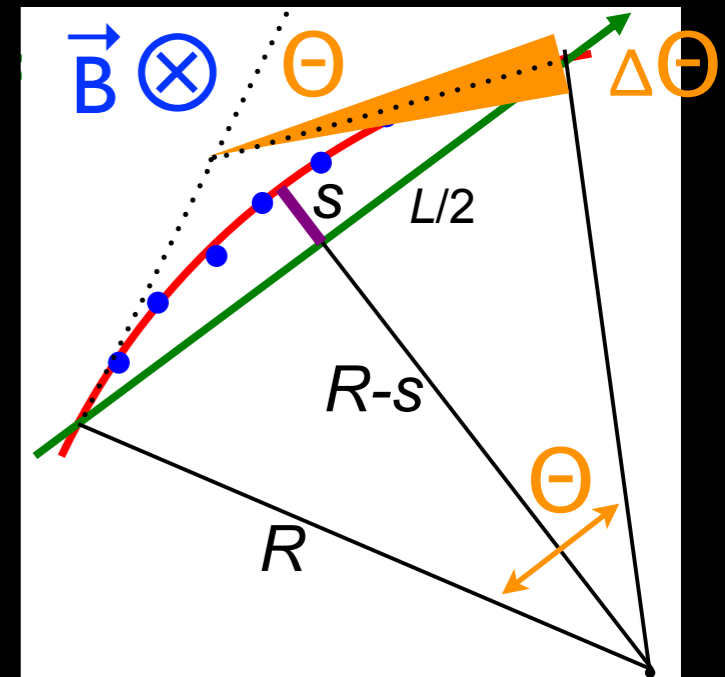
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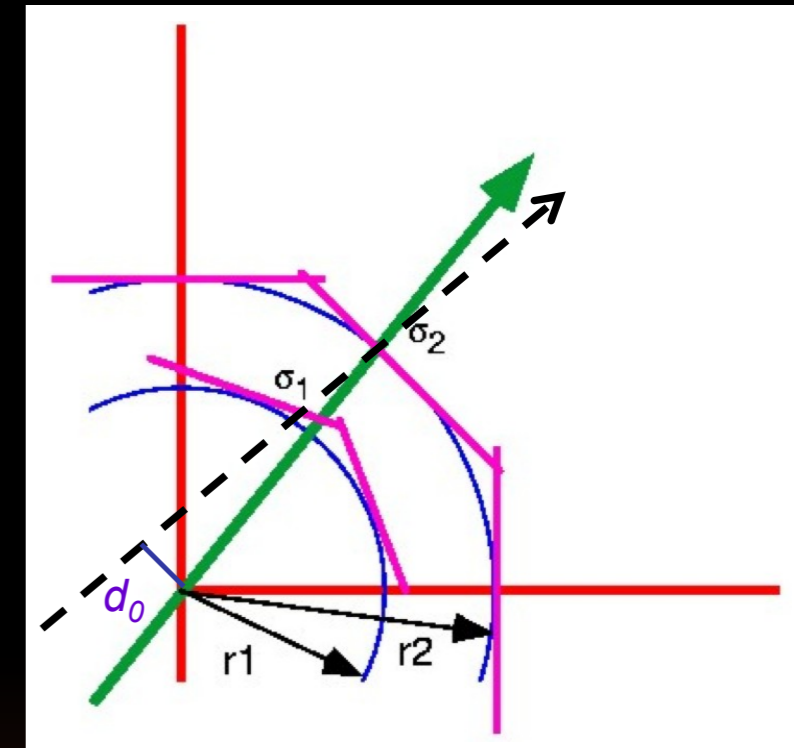
Effect on Impact Parameter Resolution

- uncertainty on the transverse impact parameter d_0

- ➔ depends on the radii and space point precision
- ➔ simplified formula for straight line and just two layers:

$$\sigma_{d_0}^2 = \frac{r_2^2 \sigma_1^2 + r_1^2 \sigma_2^2}{(r_2 - r_1)^2}$$

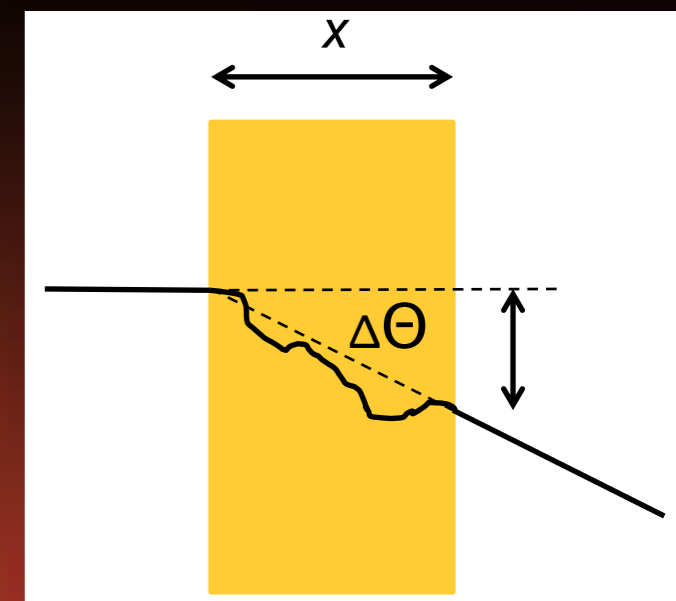
- ➔ suggests: small r_1 , large r_2 , small σ_1, σ_2



- precision is degraded by multiple scattering

$$\Delta d_0 = r \tan \Delta\Theta \approx r \Delta\Theta = r \frac{0.0136}{\beta c p} \sqrt{\frac{x}{X_0}}$$

- ➔ at low momentum scattering contribution becomes large
- ➔ best precision if small radius r and minimum thickness x

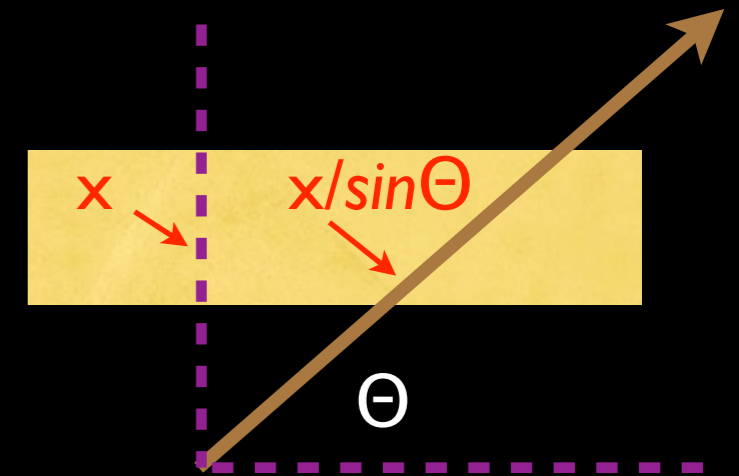


Effect on Impact Parameter Resolution

- for tracks with $\Theta \neq 90^\circ$: $r \rightarrow r/\sin\Theta$ $x \rightarrow x/\sin\Theta$

$$\sigma_{d_0} \approx \sqrt{\frac{r_2^2 \sigma_1^2 + r_1^2 \sigma_2^2}{(r_2 - r_1)^2}} \oplus \frac{r}{p \sin^{3/2} \theta} 13.6 \text{MeV} \sqrt{\frac{x}{X_0}}$$

$$\sigma_{d_0} \approx a \oplus \frac{b}{p_T \sin^{1/2} \theta}$$



- constant term describing resolution
 - multiple scattering term decreasing with p_T
- similarly momentum resolution term becomes:

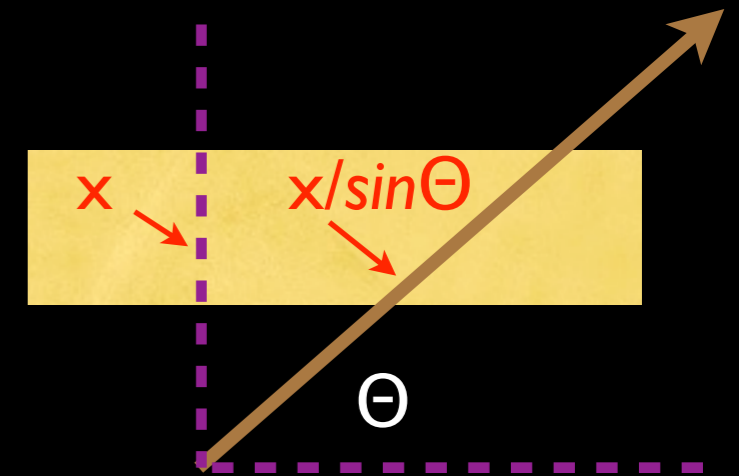
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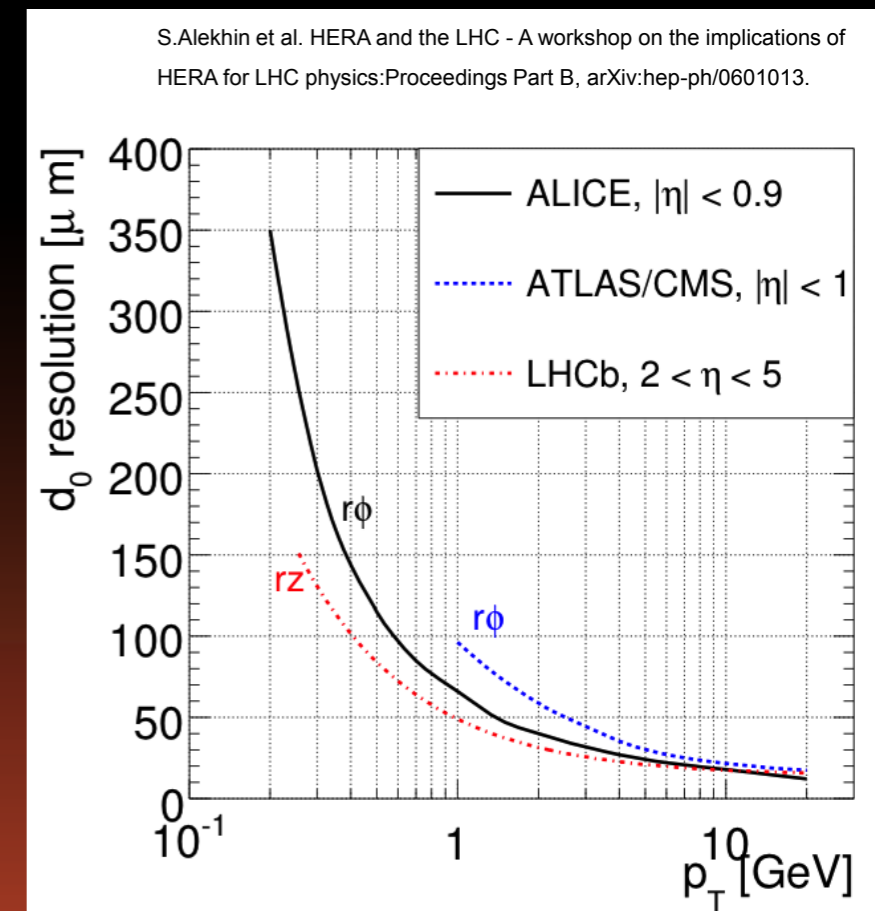
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Bremsstrahlung

- charged particle deflected by field of nucleus
 - ➔ deflecting a charged particle means “acceleration”
 - ➔ therefore radiates a photon → **Bremsstrahlung**
 - ➔ effect is strong for light particles (**electrons**), as acceleration is large for given force
 - ➔ for heavier particles (**muons**), bremsstrahlung only important at energies of a few hundred GeV (**important for ATLAS/CMS** at the LHC!)
 - ➔ presence of a nucleus is required to restore energy-momentum conservation



Bremsstrahlung

- charged particle deflected by field of nucleus



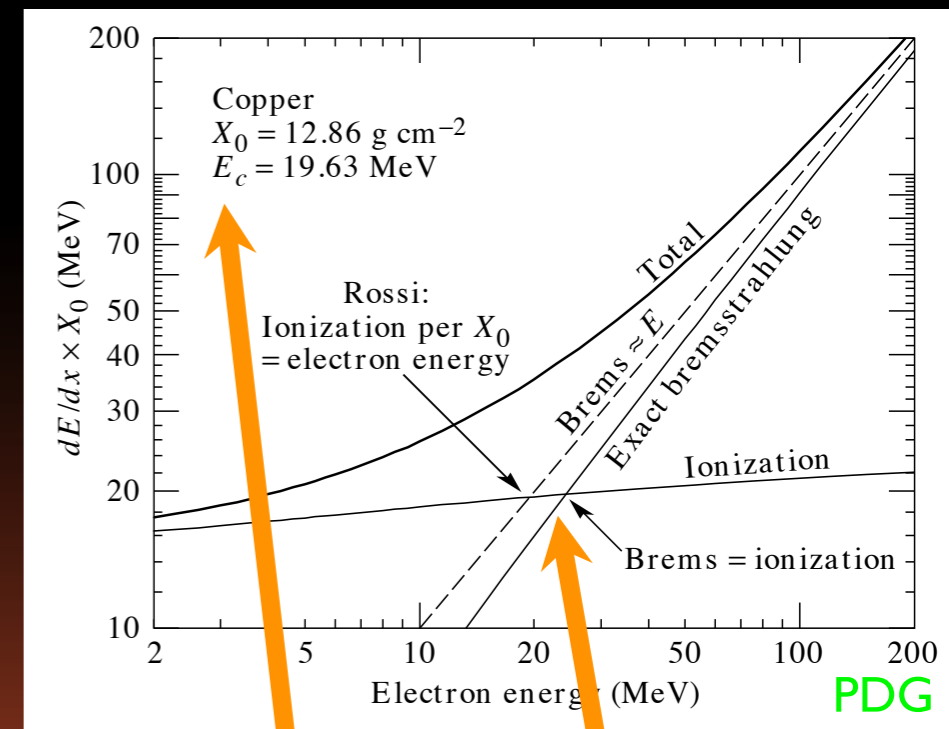
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- Bremsstrahlung proportional to

- Z^2/A and ρ of the material
- q^4 and $1/M^2$ of incoming particle
- energy lost \sim proportional to energy of particle:

$$E(x) \approx E_0 e^{-x/X_0} \quad X_0 \propto \frac{M^2 A}{q^4 \rho Z^2}$$

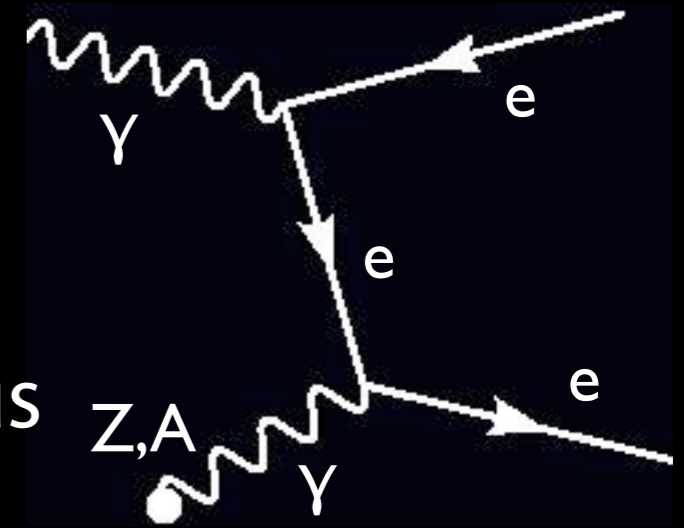
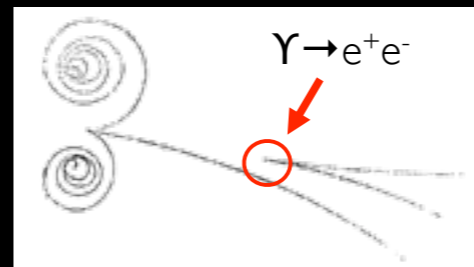
- **radiation length X_0** \sim characteristic amount of material traversed before it loses 1/e of its energy
- Bremsstrahlung of electrons in tracker material is limiting reconstruction efficiency!



important above critical energy E_c



Pair-Production



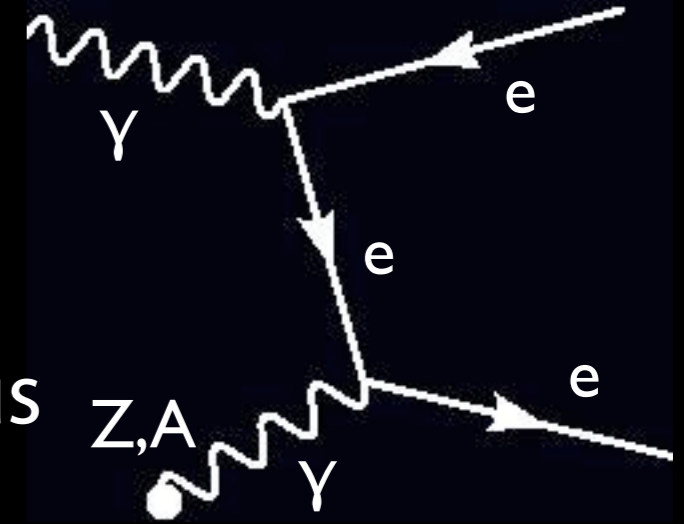
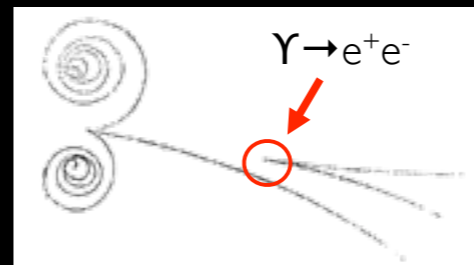
- $\gamma \rightarrow e^+e^-$ conversion process in field of nucleus

- ➔ described by diagram similar to Bremsstrahlung
- ➔ conversion probability:

$$P(x) \propto e^{-\frac{7}{9} \frac{x}{X_0}}$$

- ➔ radiation length X_0 is 7/9 of mean free path for pair production by a high energy photon
- ➔ pair production in tracker material main source of inefficiency for photons

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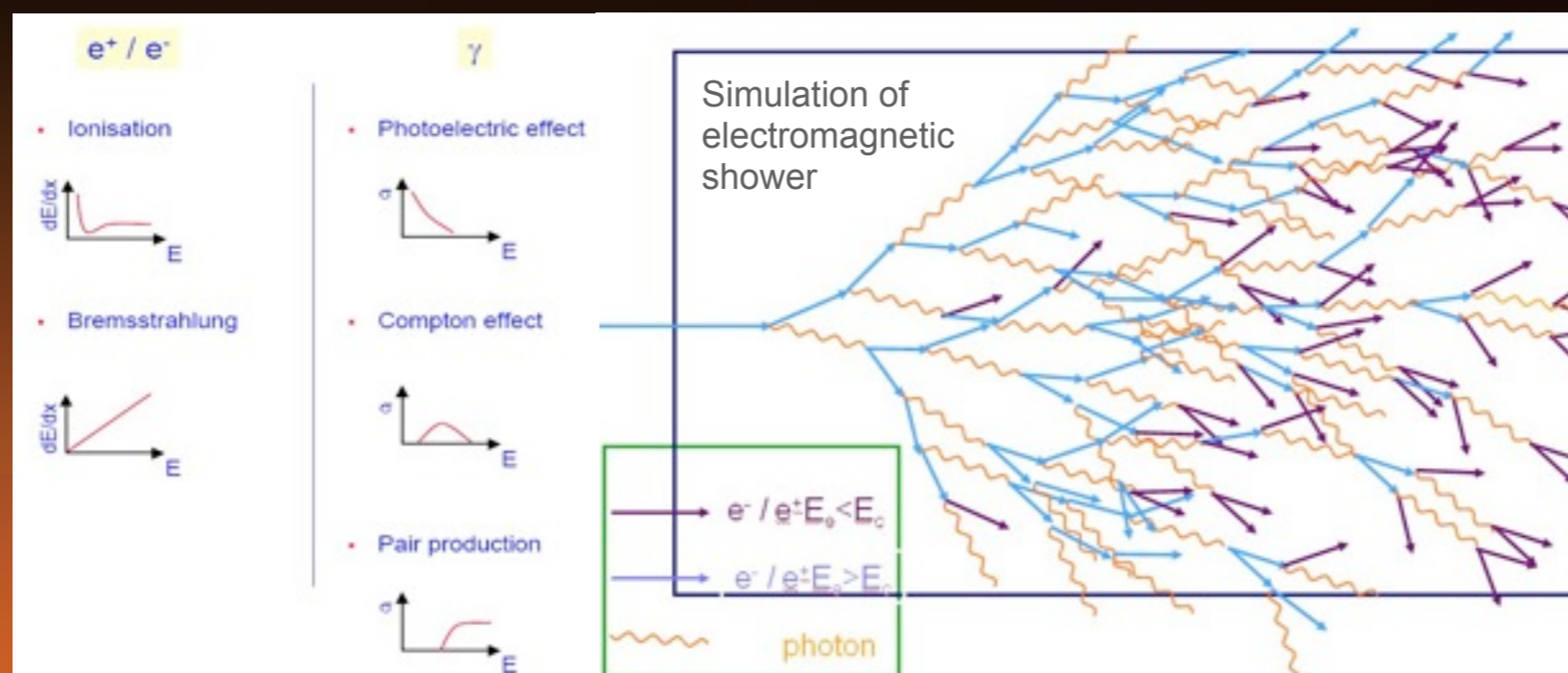
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- together they give rise to electromagnetic showers

- ➔ processes contributing to showers, detection in EM calorimeters



Hadronic Interactions

- nuclear interaction length λ : *mean free path of hadrons between strong collisions*

material	λ [cm]
Si	45.5
Fe	16.8
Pb	17.1

interactions with nuclei lead to hadronic (HAD) showers

- $\lambda > X[X_0]$, can separate EM (close) from HAD (far) showers
- detection of HAD showers in hadronic calorimeters

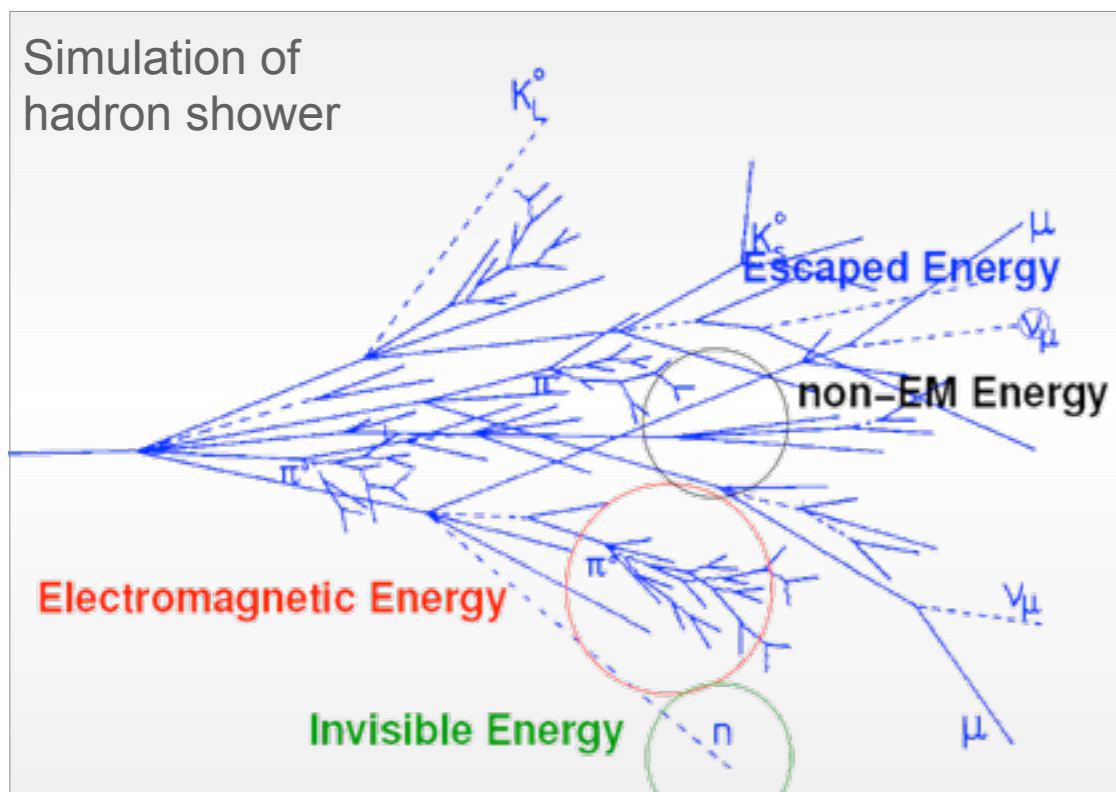
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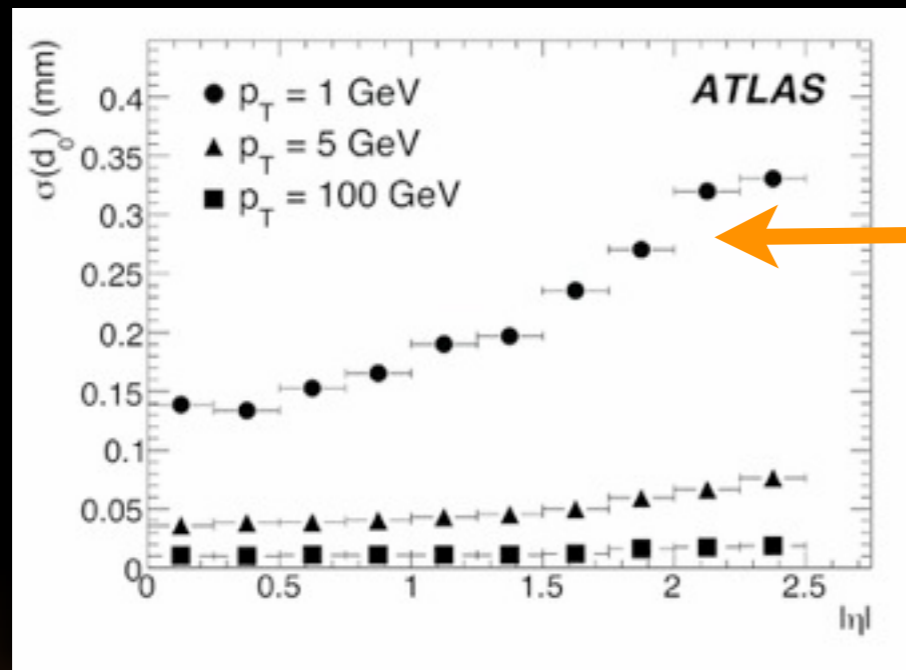
a hadronic shower consists of:

- EM energy (e.g., $\pi^0 \rightarrow \gamma\gamma$) O(50%)
- non-EM energy (e.g., dE/dx from π^\pm, μ^\pm, K^\pm) O(25%)
- invisible energy
(nuclear fission/excitation, neutrons) O(25%)
- escaped energy (e.g. neutrinos) O(2%)

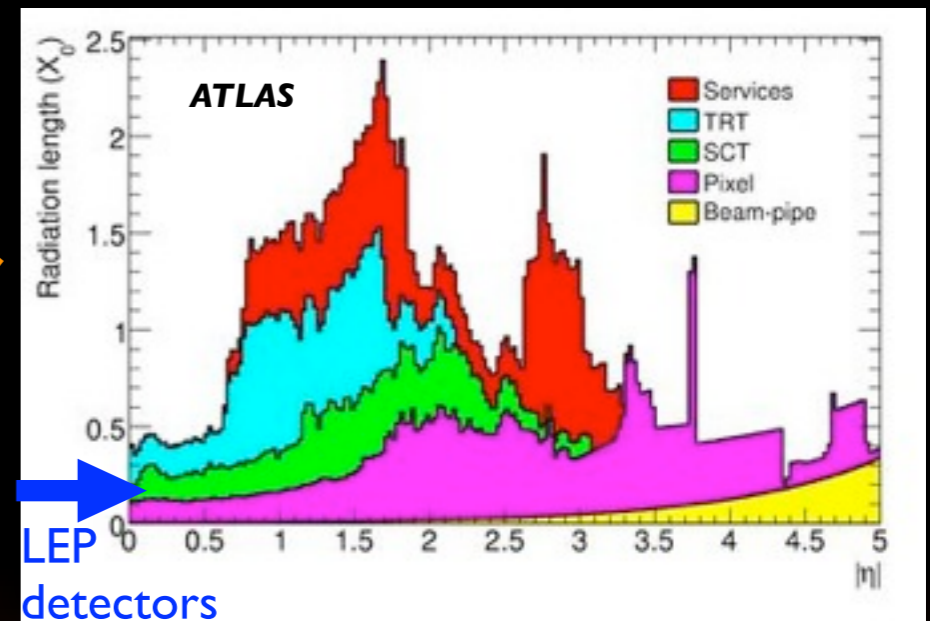
hadronic shower in **material of tracking detector** is main source of inefficiency for pions, kaons and protons !

Effect on Expected Performance

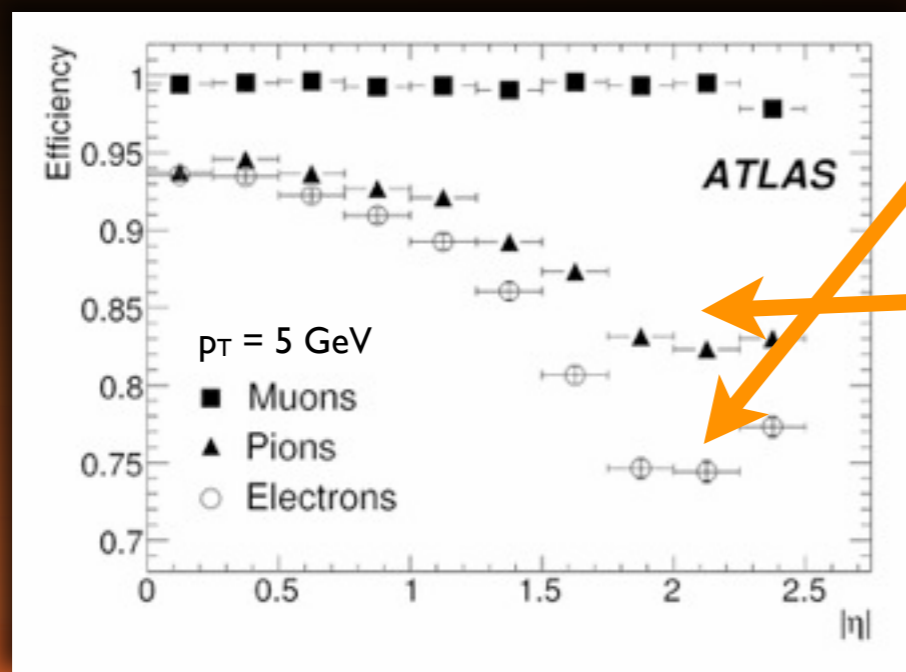
- ATLAS/CMS tracking resolution and efficiency mostly driven by interactions in detector material



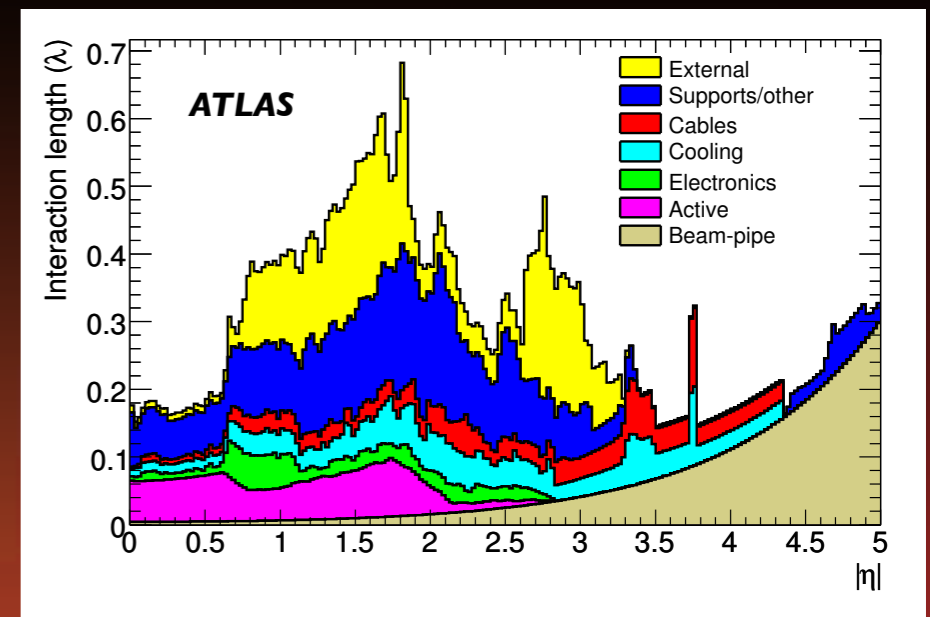
multiple scattering



LEP detectors



hadronic interactions



→ total weight of Inner Detector: 4.5 tons



Let's Summarize...

- discussed the most relevant physics processes for particles passing through (detector) material
- discussed some of the consequences
 - ➔ provide the means to detect charged particles and to identify them
 - measuring the ionization of charged particles in a medium (gas, silicon...)
 - detecting transition and Cherenkov radiation
 - ➔ as well, limiting factor for the performance of a detector
 - e.g. multiple scattering effects or effects from hadronic interactions...
- next is to talk about LHC tracking detectors

